



LRFR Calibration of Two-Strut Buckling Model for Evaluation of Compression Diagonal Gusset Plates of Steel Bridges

COMPETITIVE PAY
PENSION PROTECTION
AFFORDABLE HEALTH CARE
JOB PROTECTION
PROFESSIONAL REPRESENTATION

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Outline



Importance of Compression Gusset Plates

COMPETITIVE PAY

PENSION PROTECTION

Current Evaluation Procedures and Challenges

JOB SECURITY

PROFESSIONAL REPRESENTATION

Two-Strut Buckling (TSB) Model

Load Resistance Factor Rating (LRFR) Calibration

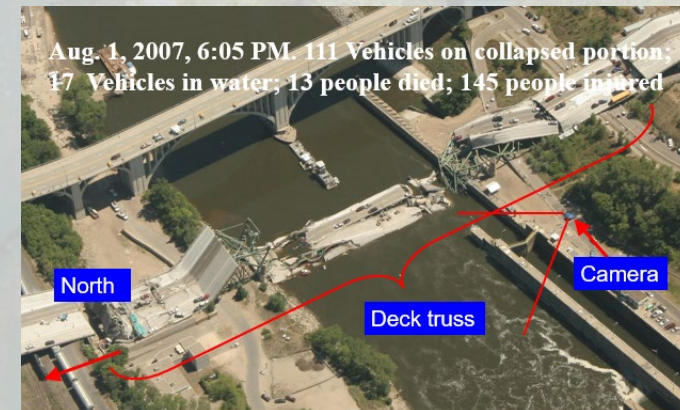
Conclusions



Importance of Compression Gusset Plates

I-35W Bridge Collapse in Minneapolis, MN August 1, 2007

- ❖ Compression Gusset Plate Design Error
- ❖ Increased Dead Load & Truck Weight
- Deck Modification – 20% increase
- Concentrated Construction Load

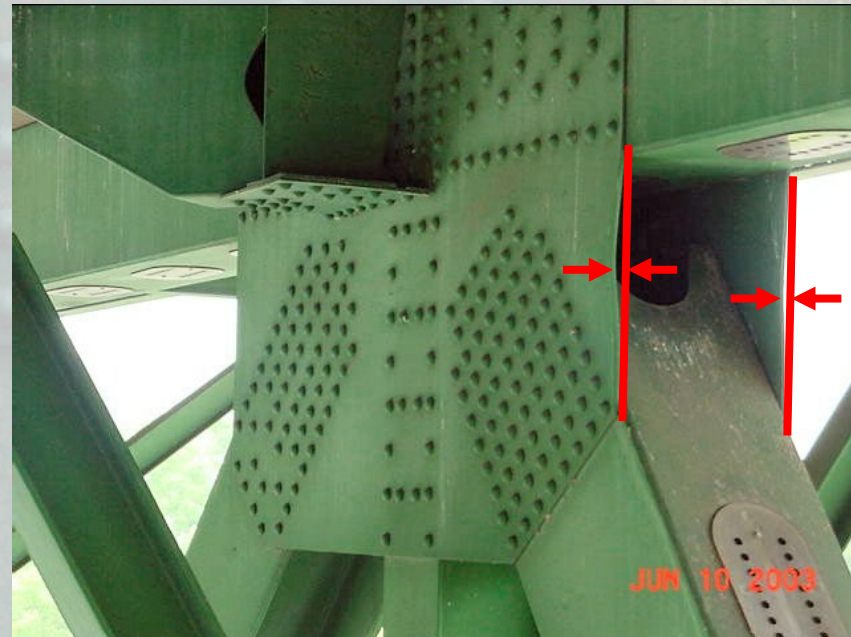


Importance of Compression Gusset Plates

I-35W Bridge Collapse in Minneapolis, MN (August 1, 2007)

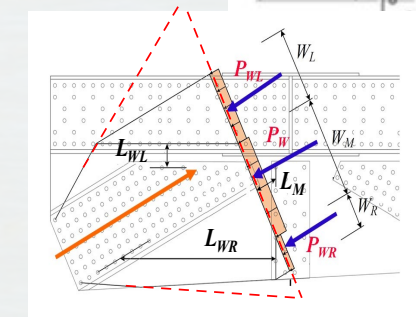
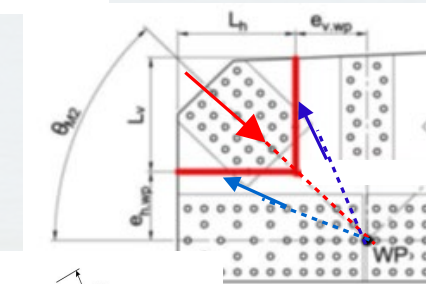
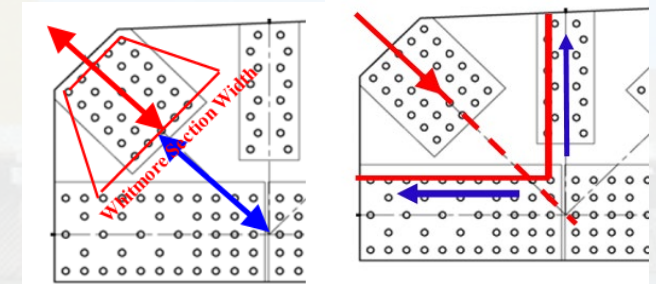
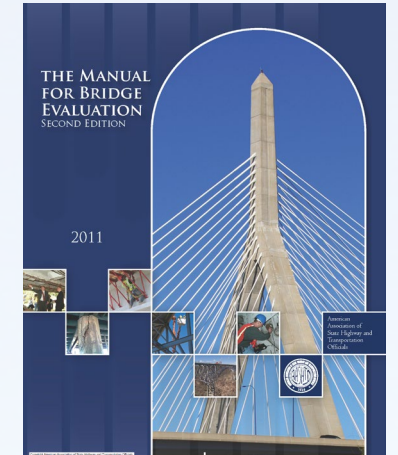
- ❖ Inadequate Attention to Compression Gusset Plates during Inspection and Load Rating Analysis
- ❖ Collapse initiated from U10E Compression Diagonal Gusset Plate

**U10E West Gusset
Plate**



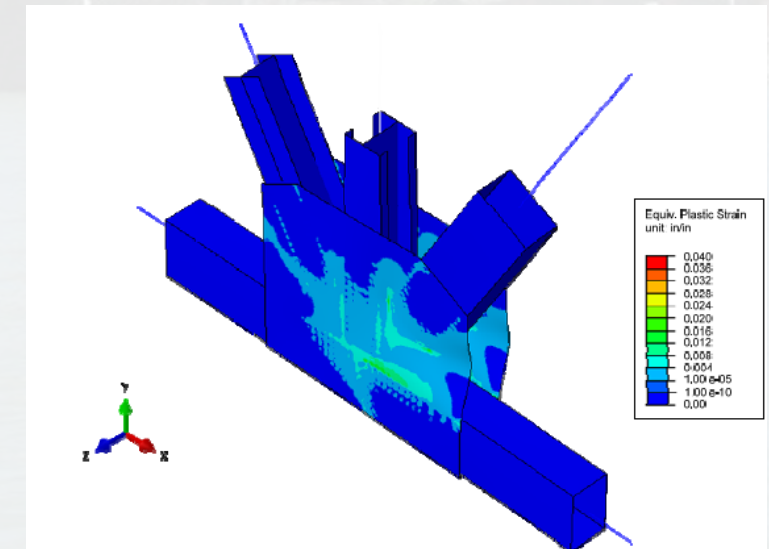
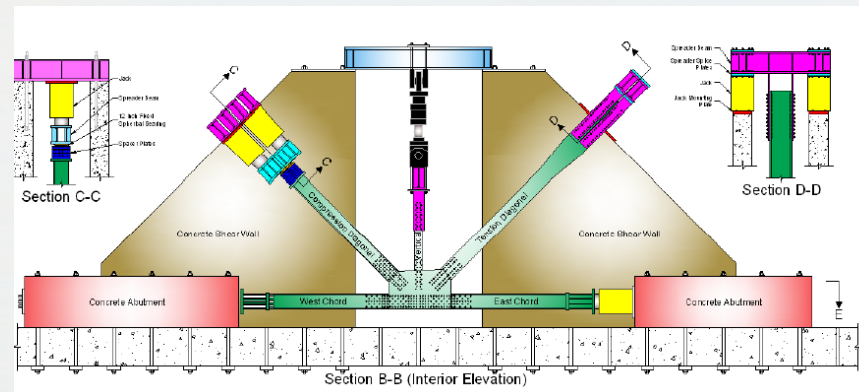
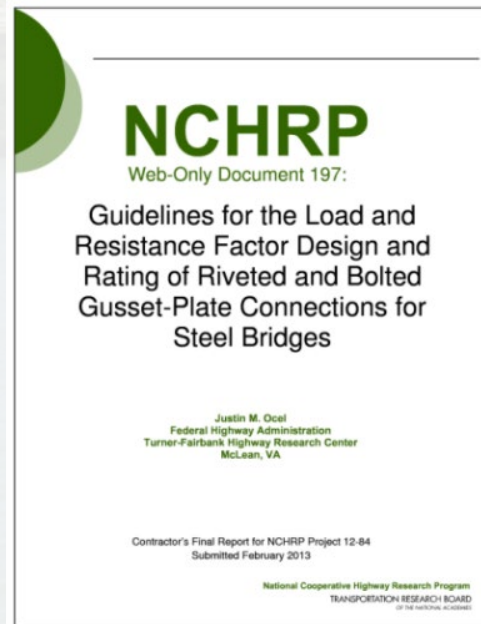
Current Evaluation Procedures and Challenges

- The Manual for Bridge Evaluation (MBE) Compression Gusset Plate Evaluation Procedure
 - First to Check - Whitmore Section Buckling and Partial Shear Plane Yielding
 - If $RF < 1.0$, then Perform Refined Analysis
 - ❖ Basic Corner Check (BCC), or
 - ❖ Truncated Whitmore Section (TWS), or
 - ❖ Nonlinear Finite Element Analysis



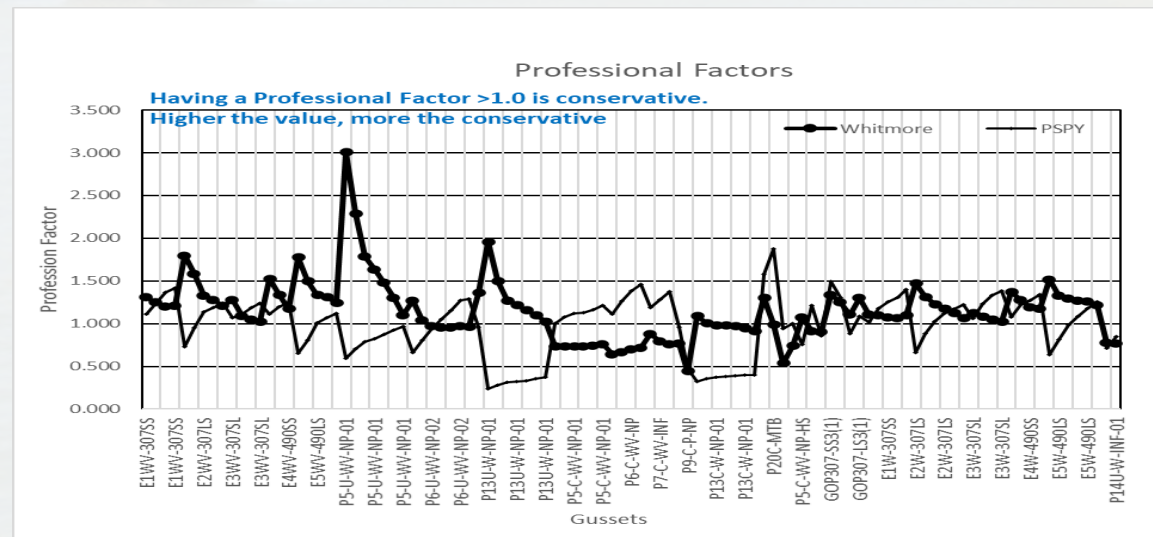
Current Evaluation Procedures and Challenges

- NCHRP Web-Only Document 197
 - Basis for gusset plate design in AASHTO LRFD BDS and evaluation in AASHTO MBE



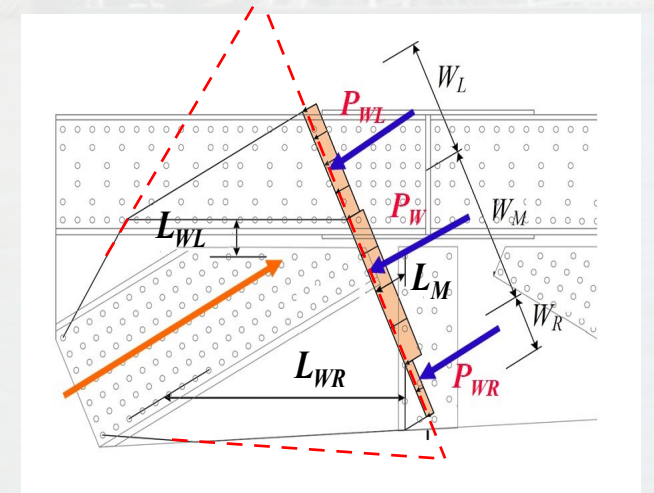
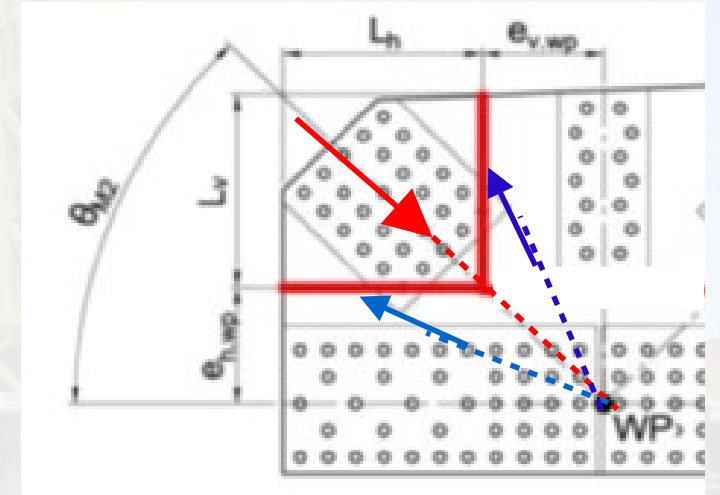
Shortcomings of Current Standard Methods

- Two-Fold Method - Generally Conservative
- While Traditional Whitmore Is Conservative, a Partial Shear Check Is Un-Conservative and Vice Versa.
- For Older Existing Bridges, this Inconsistency Results in Unnecessary Strengthening for Bridge Owners.



Shortcomings of Current Refined Methods

- Basic Corner Check (BCC)
 - Failure Surfaces Carry NO Moment
 - Force Acted Through WP
 - One of Lower Bound Solution
 - Generally Conservative
- Truncated Whitmore Section (TWS)
 - Smaller Coefficient of Variation
 - Significant Minimum PF
 - Does Not Satisfy Equilibrium
- Finite Element Analysis
 - Modeling Dependent
 - Too Complex for Ordinary Load Rating Engineers



An Example Evaluated Using Current MBE Methods

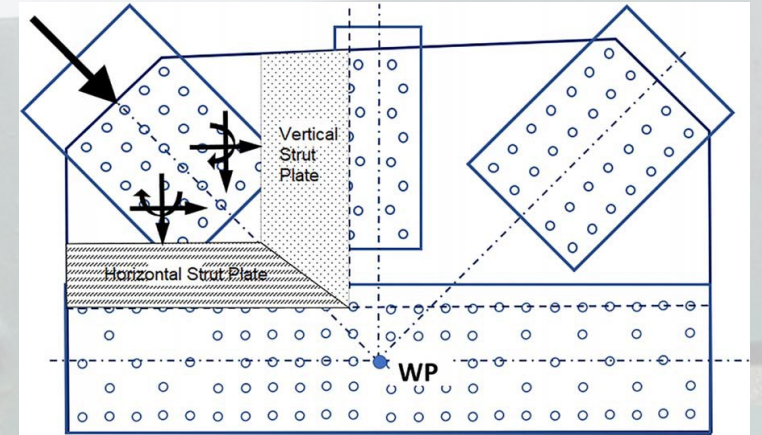
Method (Calc performed) ϕ	Whitmore $\phi_{compression}$	Partial Shear $\phi_{shear\ yielding}$	Basic Corner Check $\phi_{compression}$	Truncated Whitmore Check $\phi_{compression}$
HL93 Operating RF	1.120	-0.640	0.057 or 0.057	1.019

- Results Significantly Vary Between These Methods.
- While One Method Shows a Negative Rating, (indicate it fails under dead load). Other Method Shows Ample Capacity (rating factor of 1.019 for HL-93 loading).

Two-Strut Buckling (TSB) Model for Compression Diagonal Gusset

Main Assumptions:

- Two Struts (Vertical and Horizontal) Resist Diagonal Compression Force.
- Strut Plates Carry Different Forces and Satisfy Equilibrium.
- Strut Plates Buckle under a Specific M-P-V Interaction Equation.
- Lower Bound Theorem of Limit Analysis

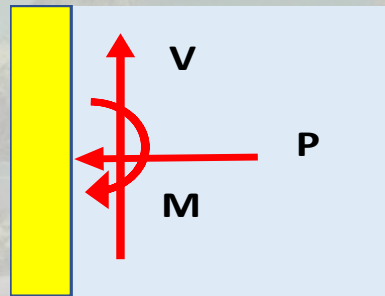


(Duan, L. and Vinayagamoorthy, M. (2023) "Limit Analysis for Evaluation of Compression Diagonal Gusset Plates in Steel Truss Bridges," *ASCE Journal of Bridge Engineering*, 28(9): 04023056-01-11)

TSB Model for Compression Diagonal Gusset

M-P-V Interaction Equation:

- Overview: mathematical equations to model how the moment (M), axial force (P), and shear force (V) interact in the two-strut plates.
- Details: equations based on previous work and consider different characteristics like modulus of elasticity, gusset plate thickness, and nominal resistances.



$$\frac{M}{M_n} + \left(\frac{P}{P_n}\right)^2 + \frac{\left(\frac{V}{V_n}\right)^4}{\left(1 - \left(\frac{P}{P_n}\right)^2\right)} = 1.0$$

TSB Model for Compression Diagonal Gusset

Comparison with BCC and TWS model (Professional Factor and COV) :

➤ Based on 116 Gusset Specimens

All gusset configurations		
Method	Mean ($P_{test}/P_{predicted}$)	COV
BCC	1.228	0.292
TWS	1.081	0.090
TSB	0.996	0.103

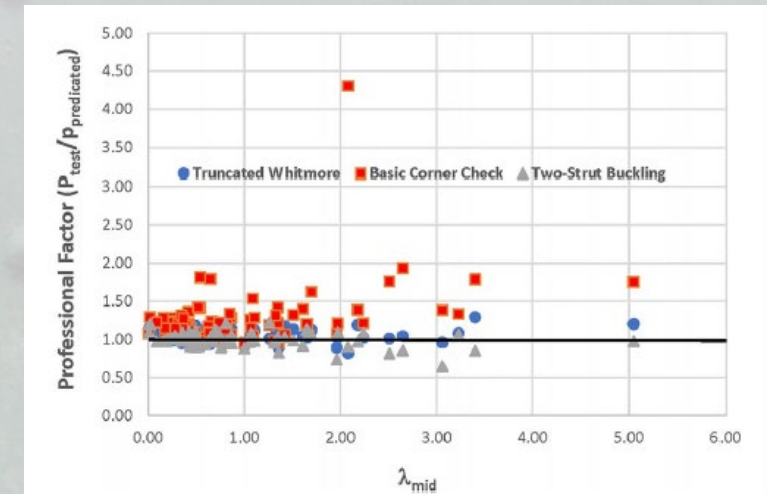


Fig. 5. PF for NCHRP 12-84 analytical tests (gusset plates with vertical member).

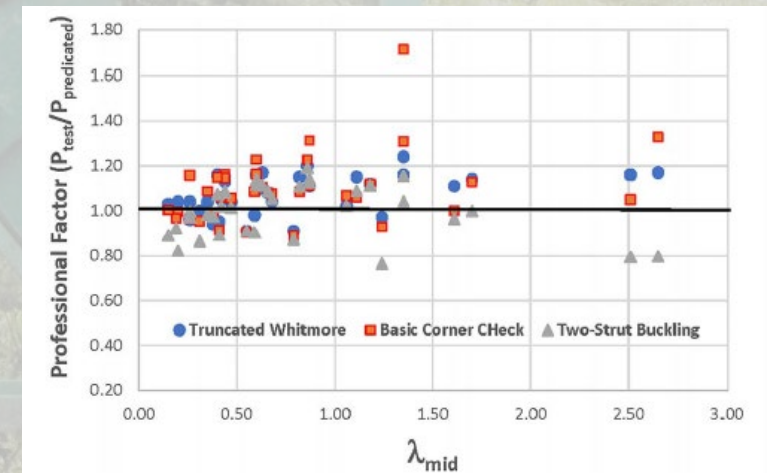


Fig. 6. PF NCHRP 12-84 analytical tests (gusset plates without vertical member).

LRFR Resistance Factor Calibration Principles

Calibration Principles used in Load Resistance and Factor Design (LRFD) Specifications:

- LRFD design specifications are Level 1 Codes. These Codes Use Deterministic Design Formulas.
- The Safety Margin is Introduced Through Partial Safety Factors (Load and Resistance Factors).
- Design Equation “ $\phi R_n \geq \sum \gamma_i Q_{ni}$ ”
- The Partial Safety Factors ϕ and γ Calibrated Based on the Target Reliability Index, β_T

LRFR Resistance Factor Calibration Principles

For Gusset Plate ONLY:

According to NCHRP Web-Only Document 197, Strength I Limit State, the Inventory Level, the Target Reliability Index, β_T is set to 4.5 for Design, while for the Operating Level, the Corresponding β_T is 3.5 for Evaluation/Rating.

LRFR Resistance Factor Calibration

Design Formula in AASHTO LRFD:

- Load & Resistance Factors Represent Partial Safety Margins

$$\gamma_D DL + \gamma_L (LL + IL) \leq \phi R$$

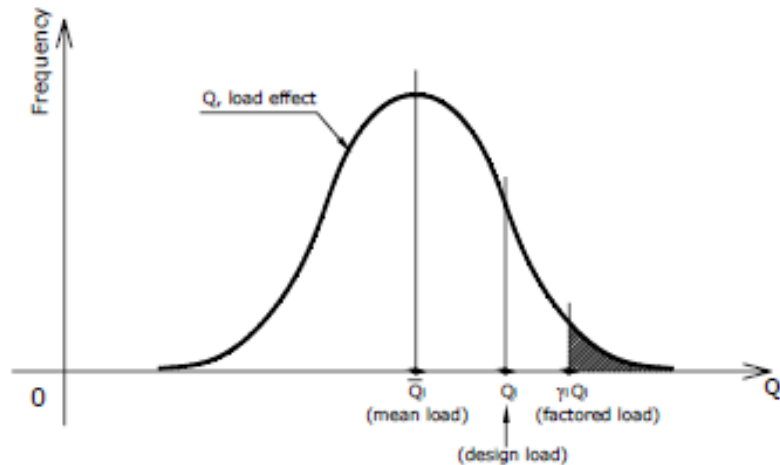


Figure 1 - Mean Load, Design (Nominal) Load and Factored Load

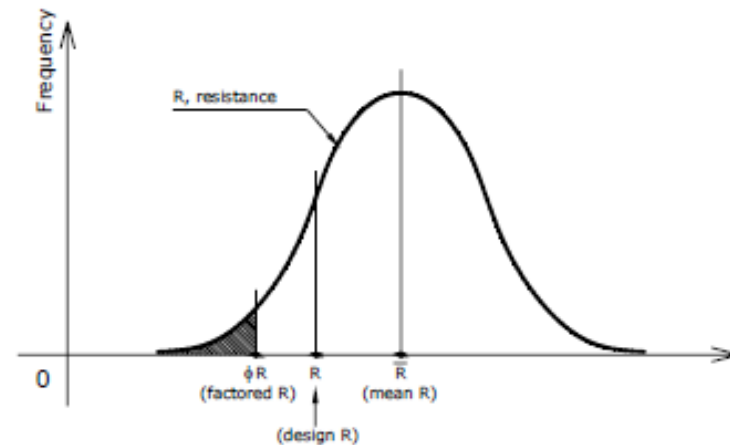


Figure 2 - Mean Resistance, Design (Nominal) Resistance and Factored Resistance

LRFR Resistance Factor Calibration

Methods to Determine Reliability Index:

- According to NCHRP Web-Only Document 197,
 - Perform Monte Carlo Simulation to Conduct a Total of 3,000,000 limit state Checks and Verify to Have 10 Failures with a Probability of Failure ($\beta_T = 4.5$)
 - The Manual for Bridge Evaluation (MBE) Gusset Plate Ratings use Monte Carlo Simulation Calibration

LRFR Resistance Factor Calibration

Calibration Process and Method:

- Model Resistance in the Form of $R = (M)(F)(P)(R_n)$
Resistance Factor Needs to be Established to a Target Reliability Index, β_T according to LRFD Design Specifications.
 - M = variation factor in material properties.
 - F = uncertainties factor in the fabrication in terms of dimensions.
 - P = professional factor = test capacity / predicted capacity
 - R_n = nominal resistance

LRFR Resistance Factor Calibration

Statistical Parameters for Loads, Materials, Fabrication :

Table 32 Assumed Calibration Statistics

	Bias Factor (λ)	COV
Dead Load	1.05	0.10
Live + Impact	1.15	0.12
Yield or Tensile Strength (F_y or F_u)	1.10	0.11
Fabrication Factor (F)	1.00	0.05

M-factor

F-factor

$$\mu_{DL} = (\lambda_{DL})(DL_n) ; \sigma_{DL} = (\mu_{DL})(V_{DL})$$

$$\mu_{LL} = (\lambda_{LL})(LL_n) ; \sigma_{LL} = (\mu_{LL})(V_{LL})$$

from NCHRP Web-Only Document 197

$$R = (R_n)(M)(P)(F)$$

$$\lambda_R = (\lambda_M)(\lambda_P)(\lambda_F)$$

$$(V_R)^2 = (V_M)^2 + (V_P)^2 + (V_F)^2$$

$$\mu_R = (\lambda_R)(R_n)$$

$$\sigma_R = (\mu_R)(V_R)$$

Results of Resistance Factors Study of TSB Model

Summary of Exact Resistance Factors:

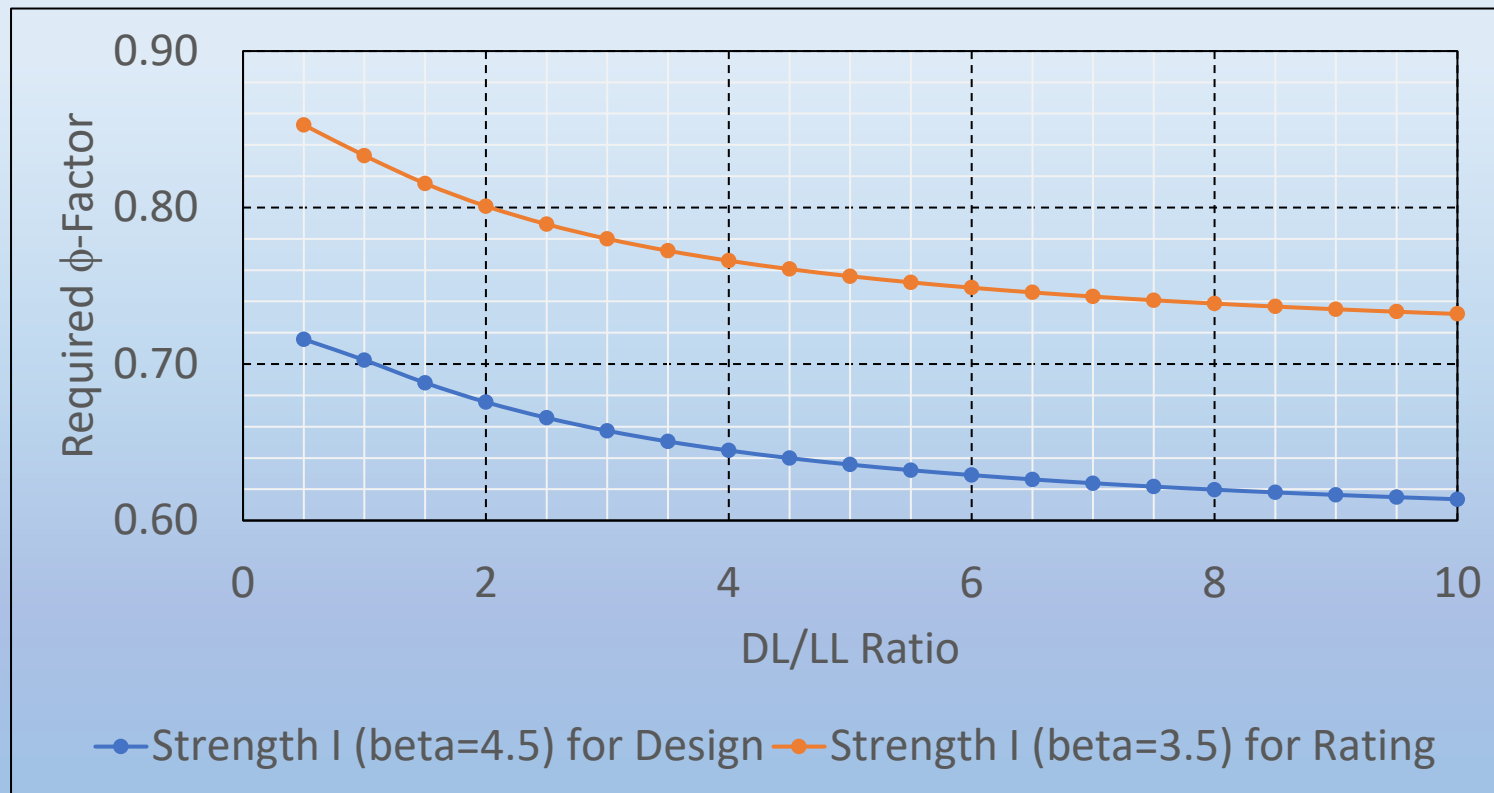
$\gamma_{LL} = 1.75$ (Strength I - HL-93 loading)

Reliability Index	$\beta_T = 4.5$				$\beta_T = 3.5$				$\beta_T = 2.5$			
DL/LL ratio	0.5	1.0	2.0	6.0	0.5	1.0	2.0	6.0	0.5	1.0	2.0	6.0
$t \geq 3/8''$	0.72	0.70	0.68	0.63	0.85	0.83	0.80	0.75	1.02	0.99	0.95	0.89
$t < 3/8''$	0.64	0.63	0.61	0.57	0.78	0.76	0.73	0.68	0.94	0.92	0.88	0.83

Results of Resistance Factors Study of TSB Model

Required ϕ -factor for Plate $\geq 3/8$ "

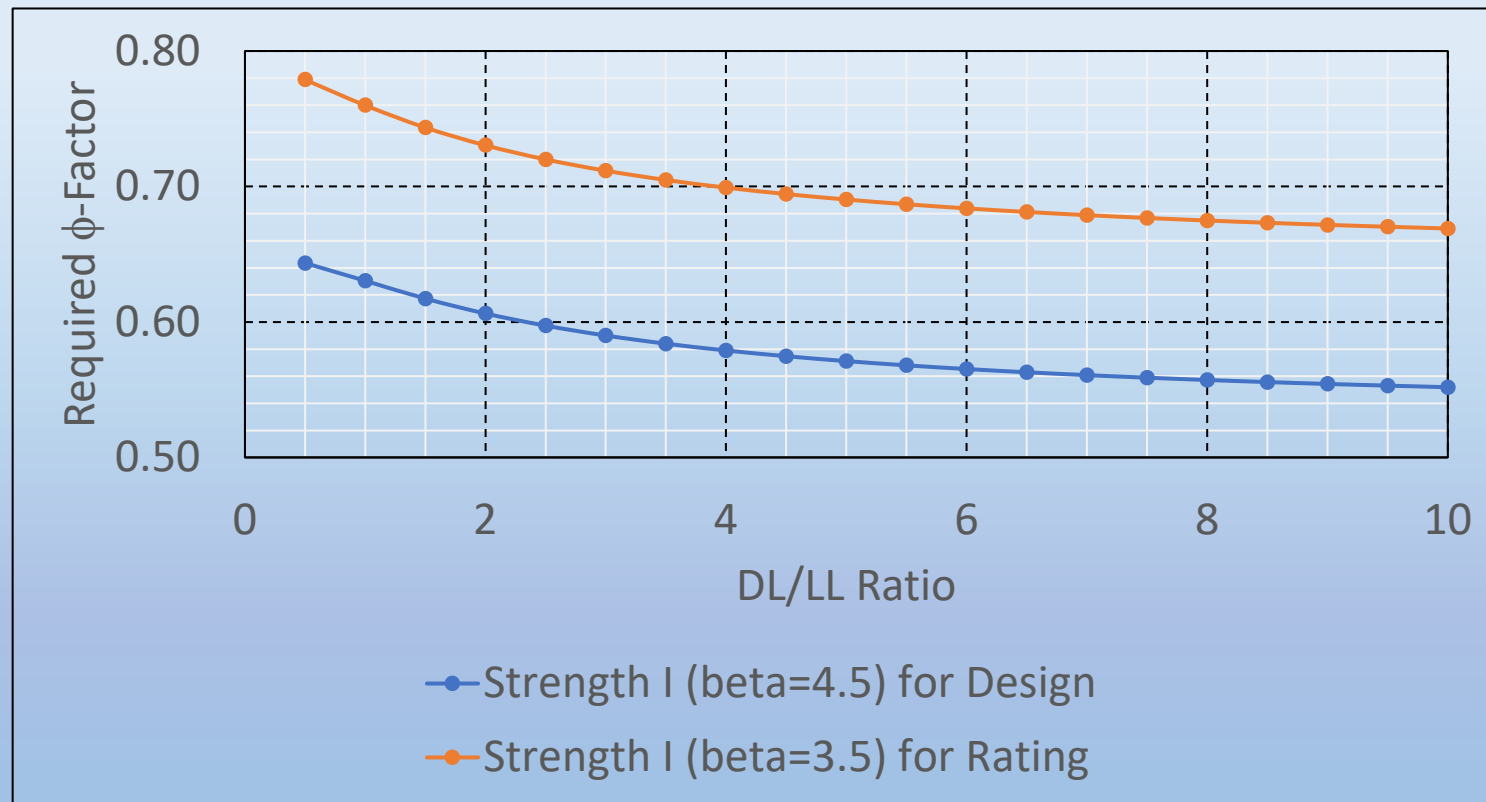
$\gamma_{LL} = 1.75$ (Strength I - HL-93 loading)



Results of Resistance Factors Study of TSB Model

Required ϕ -factor for Plate $< 3/8$ "

$\gamma_{LL} = 1.75$ (Strength I - HL-93 loading)



Results of Resistance Factors Study of TSB Model

Reliability Index (β_T) for selected ϕ -factor for Strength I
(Design & Evaluation)

$\gamma_{LL} = 1.75$ (Strength I - HL-93 loading)

	Reliability Index, β_T							
DL/LL ratio	0.5	1	2	3	4	6	8	Notes
$\phi = 0.70$ (for Design)	4.63	4.52	4.29	4.13	4.02	3.89	3.81	$t \geq 3/8''$
$\phi = 0.80$ (for Rating)	3.86	3.74	3.51	3.35	3.25	3.12	3.05	$t \geq 3/8''$
$\phi = 0.75$ (for Rating)	3.70	3.57	3.36	3.22	3.13	3.02	2.95	$t < 3/8''$



Conclusions

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- The Manual for Bridge Evaluation Two-Fold Whitmore Section Buckling (Whitmore) and the Partial Plane Shear Yielding (PPSY) are overly conservative and may result in unnecessary strengthening and retrofitting.
- Of three Refined Methods (Basic Corner Check - BCC, Truncated Whitmore Section – TWS, and Two-Strut Buckling - TSB), TSB has the best professional factor and the relatively low coefficient of variation (COV).



Conclusions

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- Based on LRFR Resistance Factor Calibration Principles, Resistance Factors for TSB Model Can Be Codified for Application
 - For Design, $\phi = 0.70$
 - For Evaluation, $\phi = 0.75$ for $t < 3/8''$;
 $\phi = 0.80$ for $t \geq 3/8''$

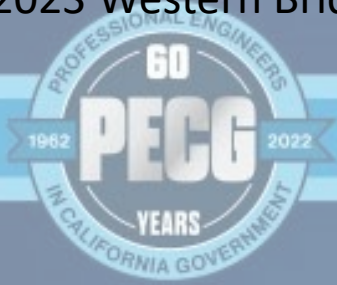


Acknowledgments

PROFESSIONAL ENGINEERS | AFFORDABLE HEALTH CARE | JOB PROTECTION | PROFESSIONAL REPRESENTATION

- Professional Engineers in California Government (PECG) Sponsored this Presentation
- ASCE Journal Peer Reviewers Recommended LRFR Calibration of Two-Strut Buckling (TSB) Model for Codified Application
- Dr. Justin Ocel of FHWA Provided NCHRP 12-84 Gusset Plate Calibration Development Background





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Thank you!

Questions?