

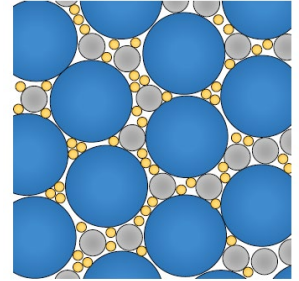
Design tools for UHPC Pretensioned Bridge Girders

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Western Bridge Engineers' Seminar, September 2023

What is UHPC?

- Ultra-High-Performance Concrete
- Composite cementitious matrix (concrete)
- No coarse aggregates
- Steel fibers for tensile strength
- Low water/binder ratio
- Particle packing
- Self consolidating (superplasticizers)



What does UHPC offer?

- Durability
- High compressive strengths (17.5 – 36 ksi)
- Tensile strength (0.9 - 1.8 ksi)

- Primary use has been in connections and overlays
- Worldwide, main structural components from UHPC
- Longer spans, lighter weight, less reinforcement (no stirrups)
- Link slabs
- Piles

Why do we need Structural Design Guidance?

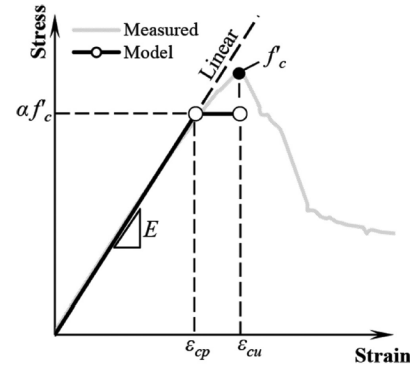
- Use of UHPC is increasing in US
- Early adopters need support and guidance for success
- Several states are looking at precast UHPC beam solutions (MN, NE, FL)
 - [Iowa, Buchanan County, Pi Girders, ASPIRE Winter 2010](#)
 - [Michigan, St. Clair County, August 2023, ABC-UTC presentation](#)
- Behavior of UHPC is different than conventional concrete
 - Strain is the limiting behavior
 - Can't use higher UHPC f'_c in LRFD equations
 - LRFD BDS does not account for UHPC tension strength
 - UHPC failure modes not accounted for in LRFD BDS

AASHTO UHPC Guide Specification

- Balloted and passed by AASHTO COBS, May 2023
- Adopts AASHTO LRFD BDS and replaces Section 5 (Concrete)
- Minimum UHPC Properties
 - $f'_c = 17.5 \text{ ksi}, f'_{ci} = 14 \text{ ksi}$
 - Cracking strength, $f_{t,cr} = 0.75 \text{ ksi}$
 - Crack localization strength, $f_{t,loc} \geq f_{t,cr}$ (Sustained post-cracking tension strength)
 - Crack localization strain, $e_{t,loc} = 0.0025$
- Fibers must be steel (secondary fibers of other types permitted)
- Tension properties characterized by direct tension test (AASHTO T 397)

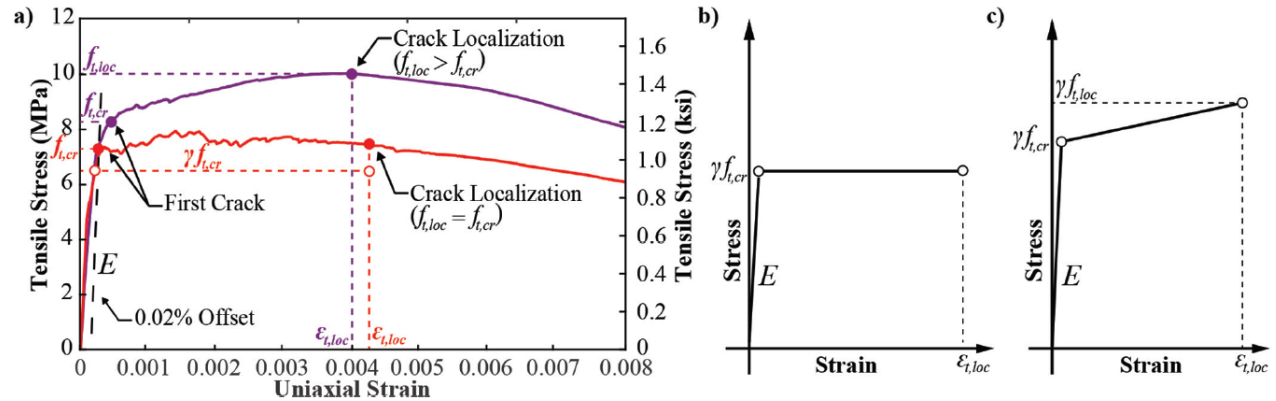
Material Models

- Compression



Source: El-Helou, et. al. ACI Materials Journal 2022

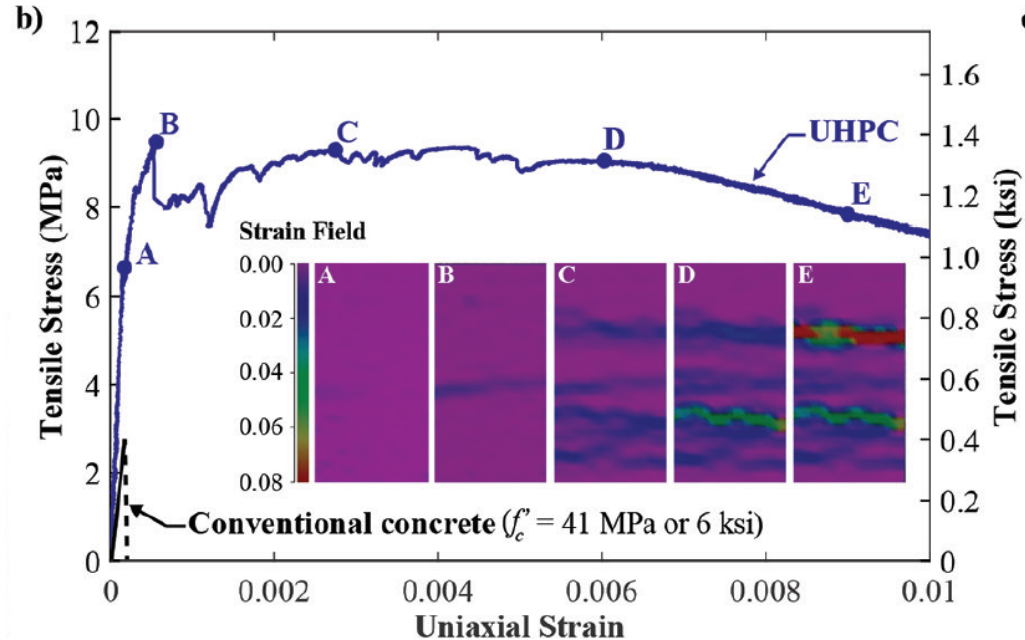
- Tension



Source: El-Helou, et. al. ACI Materials Journal 2022

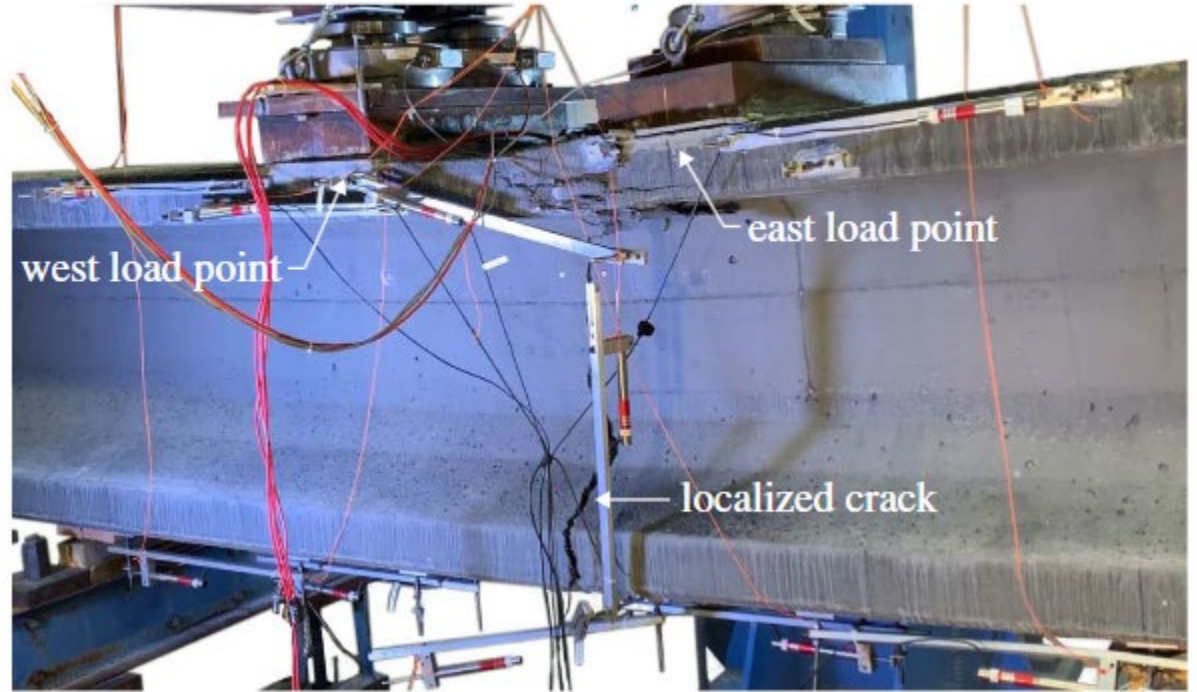
Crack Localization

- Unique failure mode
- Well distributed cracks coalesce into a single dominate crack
- Fibers are pulling out



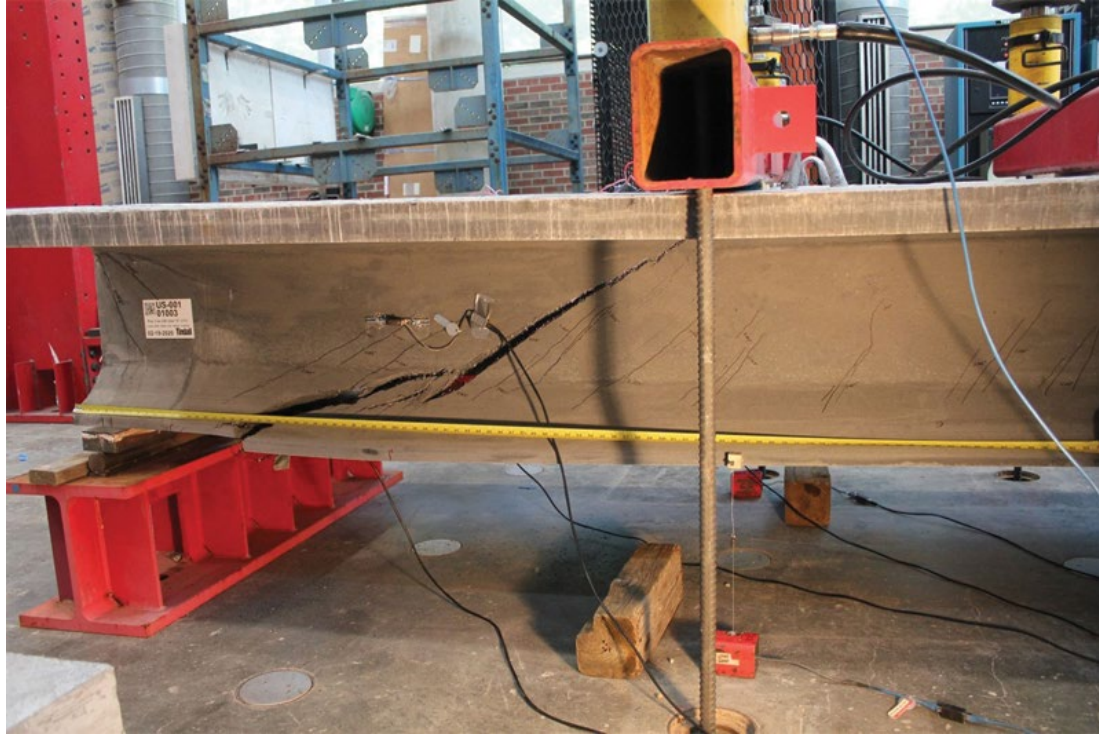
Source: El-Helou, et. al. ACI Materials Journal 2022

Crack Localization - Flexure



Source: El-Helou, et. al. ASCE J. Struct. Eng. 2022, 148(4)

Crack Localization - Shear



Service Limit State Design

- Generally, the same as for conventional concrete
- Modulus of elasticity $E_c = 2,500K_1f'_c{}^{0.33}$
- Creep and shrinkage use similar model to LRFD BDS
 - $\Psi(t, t_i) = 1.2k_s k_{hc} k_f k_{td} k_\ell K_3$ $\epsilon_{sh} = k_s k_{hs} k_f k_{td} K_4 0.6 \times 10^{-3}$
- Compression stress limits
 - Same as LRFD BDS
- Tension stress limits
 - Temporary, $\gamma_u f_{t,cri}$
 - Permanent, $\gamma_u f_{t,cr}$
 - Cyclic loading, $0.95\gamma_u f_{t,cr}$ (fatigue of fibers is a concern – limited research)
 - Reinforcement fatigue checks apply

Transfer and Development

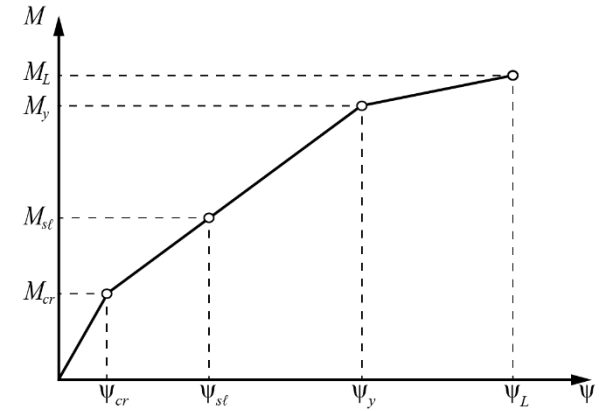
- Transfer length for prestress
 - $l_t = \xi 24d_b, \xi = 0.75 \text{ or } 1.0$
- Development length for prestress
 - $l_d \geq l_t + 0.30(f_{ps} - f_{pe})d_b$
- Development length for reinforcement
 - $l_d = \begin{cases} 10d_b & f'_c < 75\text{ksi} \\ 12d_b & 75\text{ksi} \leq f'_c \leq 100\text{ksi} \end{cases}$

Strength Limit States

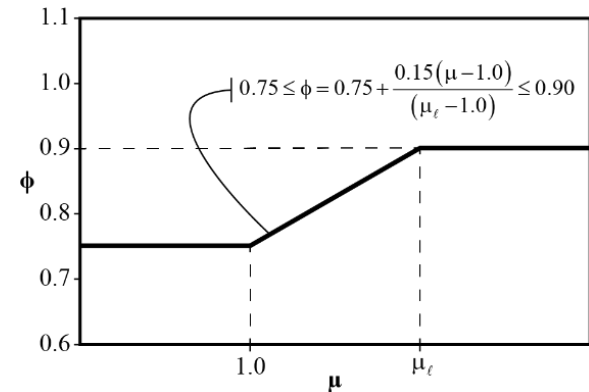
- UHPC tensile properties affect the strength limit state
- Crack localization strength typically governs strength of members
- Flexure and shear capacity analysis is considerably different than LRFD BDS
 - Whitney stress block is not valid
 - Concrete crushing strain may not be the limiting value

Flexural Capacity

- Moment curvature response computed using strain compatibility
- Governing failure mode can be
 - Composite concrete crushing (deck)
 - UHPC crushing
 - Reinforcement rupture
 - UHPC crack localization
- Resistance factor accounts for ductility in terms of curvature prior to failure limit, $\mu = \Psi_L / \Psi_{sl}$
 - 0.75 when localization controls
 - 0.90 otherwise ($\mu_l = 3$)



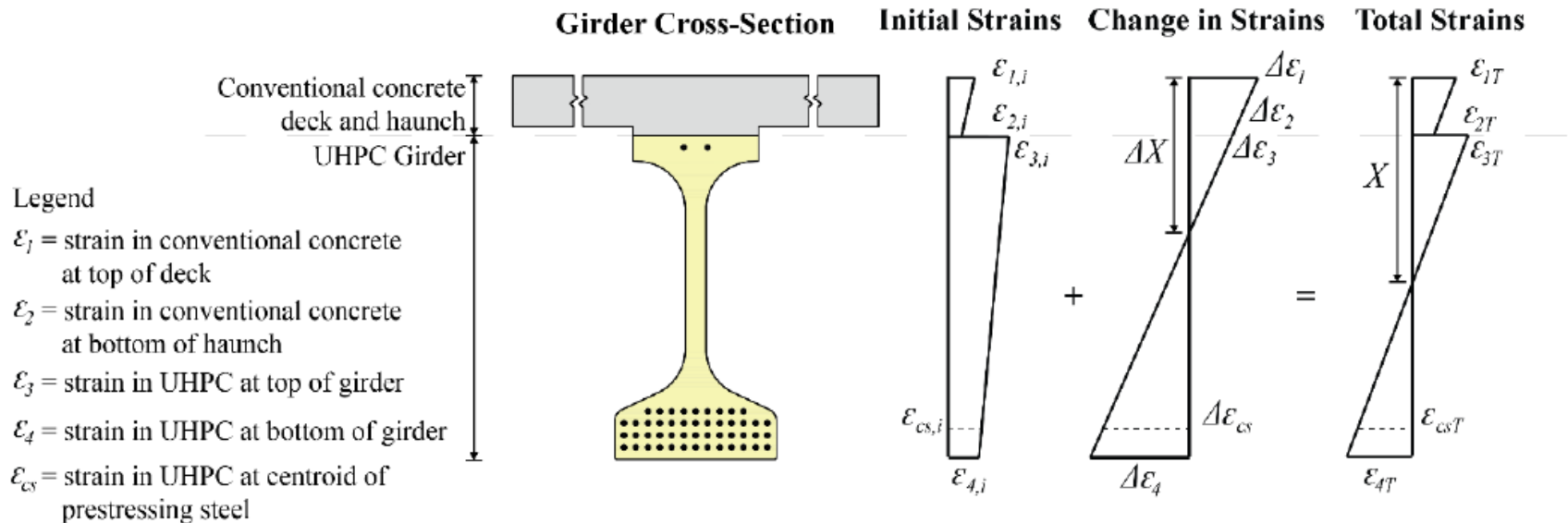
Moment curvature



Resistance factor

Strain Compatibility

- Must account for initial strains (generally ignored for conventional concrete)



Shear Capacity

- Capacity based on MCFT
- $V_n = V_{UHPC} + V_s + V_p$
- $V_{UHPC} = \gamma_u f_{t,loc} b_v d_v \cot \theta$
- $V_s = \frac{A_v f_{v,\alpha} d_v \cot \theta}{s}$
- $f_{v,\alpha}$ = stress in reinforcement at crack localization (may be less than f_y)
- Reduction factor, $\phi = 0.9$ (Same as LRFD BDS)

Shear Parameters, $f_{v,\alpha}$ and θ

- Iterate design equations to determining $f_{v,\alpha}$ and θ
- Guess $f_{v,\alpha} = f_y$, solve for θ
- Compute ε_2 , ε_v , and $f_{v,\alpha}$
- Repeat until convergence
- Simplified method using tables in appendix

$$\gamma_u \varepsilon_{t,loc} = \frac{\varepsilon_s}{2} (1 + \cot^2 \theta) + \frac{2f_{t,loc}}{E_c} \cot^4 \theta + \frac{2\rho_{v,\alpha} f_{v,\alpha}}{E_c} \cot^2 \theta (1 + \cot^2 \theta)$$

$$\varepsilon_2 = -\frac{2f_{t,loc}}{E_c} \cot^2 \theta - \frac{2\rho_{v,\alpha} f_{v,\alpha}}{E_c} (1 + \cot^2 \theta)$$

$$\varepsilon_v = \gamma_u \varepsilon_{t,loc} - 0.5\varepsilon_s + \varepsilon_2$$

$$f_{v,\alpha} = \frac{E_s \varepsilon_v}{\sin \alpha} \leq f_y$$

$$\rho_{v,\alpha} = \frac{A_v}{b_v s} \left(1 + \frac{\cot \alpha}{\cot \theta} \right) \sin \alpha$$

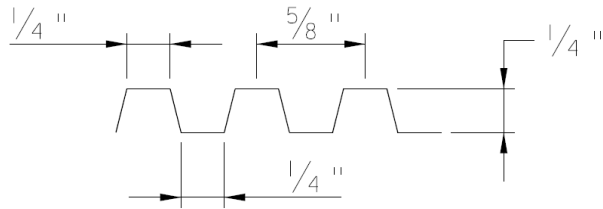
- $f_{v,\alpha}$ = stress in reinforcement
- θ = inclination of shear crack

Table B1.3-1. Values of θ (degrees) and upper limit of $f_{v,\alpha}$ (ksi) for sections with transverse reinforcement with $\rho_{v,\alpha} \leq 1.0$ percent.

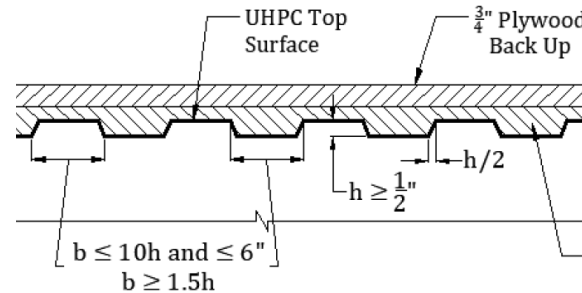
ε_s $\times 1,000$	Parameter	$\gamma_u \varepsilon_{t,loc} \times 1,000$											
		≥ 2.5	≥ 3.0	≥ 3.5	≥ 4.0	≥ 4.5	≥ 5.0	≥ 5.5	≥ 6.0	≥ 6.5	≥ 7.0	≥ 7.5	≥ 8.0
≤ -1.0	θ (deg.)	32.7	32.3	31.9	31.6	31.3	30.8	30.2	29.8	29.3	28.9	28.6	28.2
	$f_{v,\alpha}$ (ksi)	≤ 36.7	≤ 46.6	≤ 56.5	≤ 66.5	≤ 75.0	≤ 75.0	≤ 75.0	≤ 75.0	≤ 75.0	≤ 75.0	≤ 75.0	≤ 75.0
≤ -0.5	θ (deg.)	34.3	33.7	33.2	32.8	32.4	31.8	31.2	30.7	30.2	29.8	29.4	29.0
	$f_{v,\alpha}$ (ksi)	≤ 35.3	≤ 45.1	≤ 54.9	≤ 64.8	≤ 74.8	≤ 75.0	≤ 75.0	≤ 75.0	≤ 75.0	≤ 75.0	≤ 75.0	≤ 75.0
≤ 0.0	θ (deg.)	36.2	35.3	34.6	34.1	33.6	32.9	32.3	31.7	31.2	30.7	30.2	29.8
	$f_{v,\alpha}$ (ksi)	≤ 33.8	≤ 43.4	≤ 53.1	≤ 63.0	≤ 72.9	≤ 75.0	≤ 75.0	≤ 75.0	≤ 75.0	≤ 75.0	≤ 75.0	≤ 75.0

Horizontal Interface Shear

- Similar to conventional concrete, friction and cohesion factors
- UHPC is self consolidating, so surface tends to be smooth
- Roughening of UHPC surface is difficult
- Options for forming flutes or shear keys



Formed Flutes



Formed Shear Keys

Material Testing and Qualification

- Material conformance guidance is being developed (AASHTO ballot 2024)
- PCI has done significant work in material testing
- Tension properties of UHPC is important for structural behavior
- Test Methods – Flexural Prism, Direct Tension
- T-10 intends for direct tension for mix qualification with flexural prism as datum for QC testing



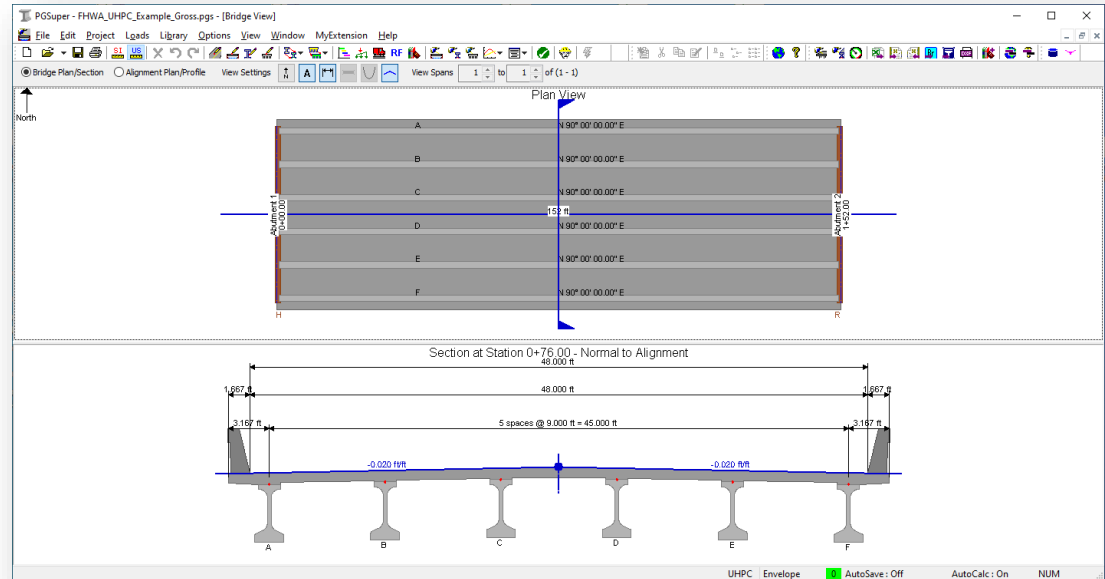
Direct Tension
AASHTO T 397



Flexural Prism
ASTM C 1609

UHPC Design with PGSuper

- PGSuper 8.0 Beta
- Support for UHPC class materials in prestress components
- Evaluates service, fatigue, and strength limit states
- Performs flexural analysis with strain compatibility & moment curvature
- Shear capacity using general method



Modeling UHPC

- Edit Girder
- Press [More Properties...]
- Select concrete UHPC
- Define UHPC parameters

Girder Details for Span 1, Girder A

General Strands Debonding Long. Reinforcement Trans. Reinforcement Temporary Conditions Bearings Extension Page

Events
Construction Event 1: Construct Girders, Erect Piers Erection Event 2: Erect Girders

Girder
This girder type is used in all spans
MN54-Modified

Girder Modifiers
Precamber 0.000 in

Girder Concrete Properties
Ultra High Performance Concrete (UHPC)
f'ci 14.000 KSI Eci 5972.584 KSI
f'c 22.000 KSI Ec 6933.292 KSI

More Properties...

Concrete Details

General Modifiers UHPC PCI-UHPC

Type UHPC

Strength - f'c 22.000 KSI

Unit Weight 0.155 kip/ft³

Unit Weight with Reinforcement 0.160 kip/ft³

Mod. Elasticity, Ec 6933.292 KSI

Copy from library...

Concrete Details

General Modifiers UHPC PCI-UHPC

Initial effective cracking strength (ft,cr) 0.900 KSI

Design effective cracking strength (ft,cr) 1.200 KSI

Crack localization strength (ft,loc) 1.200 KSI

Crack localization strain (et,loc) 0.004

Compressive stress-strain response reduction factor (alpha.u) 0.85

Experimentally derived ultimate compressive strain (e.cu)

Fiber orientation reduction factor (gamma.u) 1

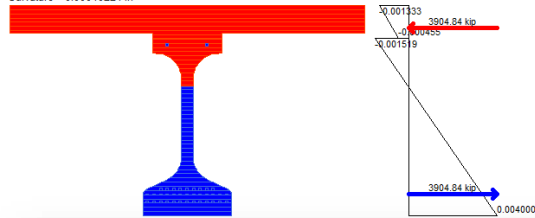
Fiber Length 0.500 in

OK Cancel Help

Flexural Strength Analysis

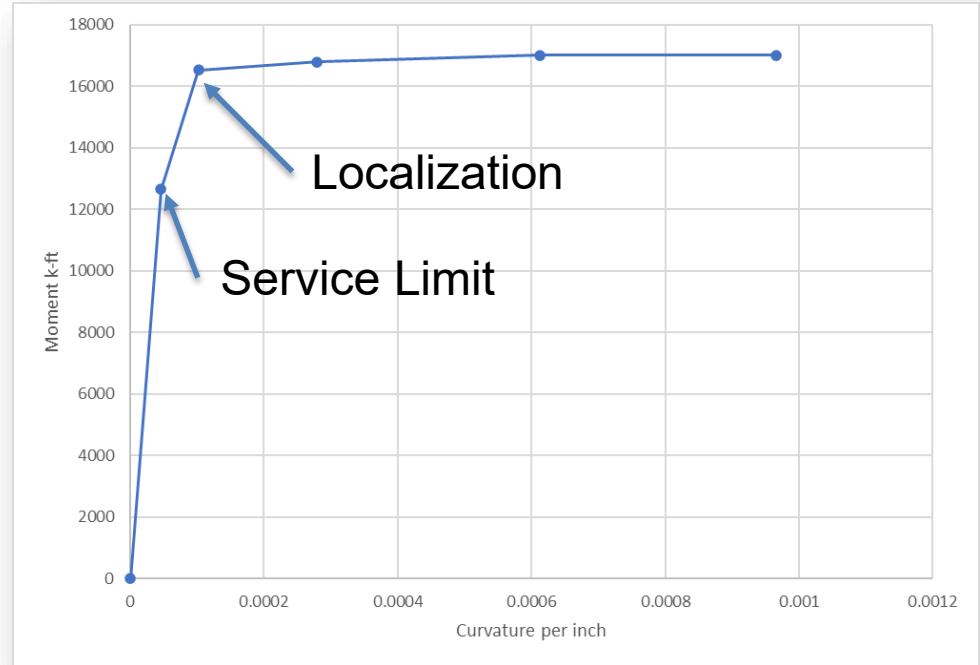
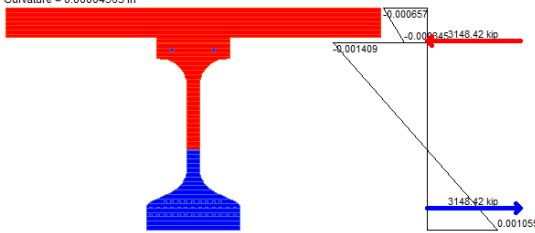
Girder UHPC crack localization

Depth to neutral axis, $c = 24.866$ in
 Compression Resultant, $C = -3904.84$ kip
 Depth to Compression Resultant, $d_c = 6.750$ in
 Tension Resultant, $T = 3904.84$ kip
 Depth to Tension Resultant, $d_t = 57.510$ in
 Nominal Capacity, $M_n = 16517.70$ kip-ft
 Moment Arm = $M_n/T = 50.761$ in
 Curvature = 0.00010221 in⁻¹



Capacity at reinforcement stress limit state

Depth to neutral axis, $c = 40.877$ in
 Compression Resultant, $C = -3148.42$ kip
 Depth to Compression Resultant, $d_c = 9.484$ in
 Tension Resultant, $T = 3148.42$ kip
 Depth to Tension Resultant, $d_t = 57.659$ in
 Nominal Capacity, $M_n = 12639.59$ kip-ft
 Moment Arm = $M_n/T = 48.175$ in
 Curvature = 0.00004583 in⁻¹



Shear Resistance Parameters

Shear Resistance Parameter - Strength I - GS 1.7.3.4

$$\gamma_u \varepsilon_{t,loc} = \frac{\varepsilon_s}{2} (1 + \cot^2 \theta) + \frac{2f_{t,loc}}{E_c} \cot^4 \theta + \frac{2\rho_{v,\alpha} f_{v,\alpha}}{E_c} \cot^2 \theta (1 + \cot^2 \theta)$$

$$\varepsilon_2 = -\frac{2f_{t,loc}}{E_c} \cot^2 \theta - \frac{2\rho_{v,\alpha} f_{v,\alpha}}{E_c} (1 + \cot^2 \theta)$$

$$\varepsilon_v = \gamma_u \varepsilon_{t,loc} - 0.5\varepsilon_s + \varepsilon_2$$

$$f_{v,\alpha} = \frac{E_s \varepsilon_v}{\sin \alpha} \leq f_y$$

$$\rho_{v,\alpha} = \frac{A_v}{b_v s} \left(1 + \frac{\cot \alpha}{\cot \theta} \right) \sin \alpha$$

Location from Left Support (ft)	$\varepsilon_s \times 1000$	$\gamma_u \varepsilon_{t,loc} \times 1000$	$f_{t,loc}$ (KSI)	E_c (KSI)	α (deg)	$\rho_{v,\alpha}$	$\varepsilon_2 \times 1000$	$\varepsilon_v \times 1000$	θ (deg)	$f_{v,\alpha}$ (KSI)
(CS) 4.939	-0.398		4 1.200	6933.292	90.00	0.00952	-1.65	2.55	30.42	60.000
(H) 5.000	-0.402		4 1.200	6933.292	90.00	0.00952	-1.65	2.55	30.41	60.000
(PSXFR) 5.550	-0.436		4 1.200	6933.292	90.00	0.00952	-1.66	2.56	30.31	60.000
(1.5H) 7.250	-0.471		4 1.200	6933.292	90.00	0.00952	-1.67	2.56	30.21	60.000
(Debond) 9.500	-0.444		4 1.200	6933.292	90.00	0.00952	-1.66	2.56	30.29	60.000
(PSXFR) 10.550	-0.451		4 1.200	6933.292	90.00	0.00952	-1.67	2.56	30.27	60.000
14.500	-0.416		4 1.200	6933.292	90.00	0.00952	-1.65	2.56	30.37	60.000

Questions?

Download BridgeLink
<https://wsdot.wa.gov/eesc/bridge/software>



Real Opportunity for Cost Savings

