

# Computer-Aided Design, Analysis and Load Rating of Precast-Prestressed Spliced Girder Bridges



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## Outline

- LRFD Requirements for Spliced Girder Bridges
- Overview of Spliced Girder Analysis
- Computer Aided Design, Analysis, and Load Rating

## Design, Analysis, and Rating of Spliced Girder Bridges

- Basic requirements of conventional precast-prestressed girder bridges
  - Service stress limitations, ultimate strength requirements, etc.
- LRFD 5.14.1.3 – Spliced Precast Girders
  - Additional requirements for contract documents
  - Additional service stress limitations
  - Additional analysis requirements

# LRFD Requirement for Time-Step Analysis

## LRFD 5.9.5.4.1

For segmental construction and **post-tensioned spliced precast girders, other than during preliminary design, prestress losses shall be determined by the time-step method... including consideration of the time-dependent construction stages** and schedule shown in the contract documents.

**For components with combined pretensioning and post-tensioning, and where post-tensioning is applied in more than one stage, the effects of subsequent prestressing on the creep loss of previous prestressing shall be considered.**

## Introduction to Time-Step Analysis

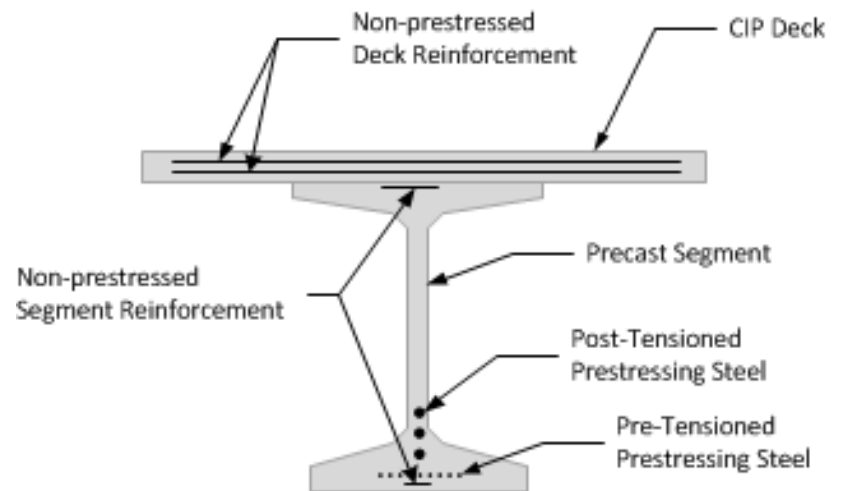
- Models design life through discrete time intervals
- Uses fundamental principles of engineering mechanics
- Accounts for time-dependent material properties and responses ( $f'_c$ ,  $\psi$ ,  $\epsilon_{shrinkage}$ , *relaxation*)
- Step-wise pseudo-linear solution to a nonlinear problem
- Structural response at the end of any interval is the summation of the responses of all the preceding intervals

## Challenge of Time-Step Analysis

- Sheer quantity of computations that must be performed
  - Deformations are computed at many locations
  - Deformations are computed in every piece of the spliced girder
  - Deformations are computed for the design life of the structure
  - Transformed section properties change with time and location
    - Non-prismatic segments (haunches, varying tendon locations)
    - $E_c$  and thus the modular ratios vary with time
  - Loading conditions change with time
    - Staged application of superimposed loads
    - Multi-staged post-tensioning
  - Statical structural system changes with time
    - Composite closure joints
    - Composite deck
    - Temporary support removal

## Composition of Spliced Girders

- Precast concrete segments
- CIP concrete closure joints and deck
- Prestressing Strands and Tendons
- Non-prestressed reinforcement



## Time Variation of Material Properties

- Three distinct materials
- Concrete
  - Strength ( $f'_c$ ) and stiffness ( $E_c$ ) vary with time
  - Creep rate varies with time and time of loading
  - Shrinkage rate varies with time
- Prestressing steel
  - Relaxation rate varies with time and loading
- Non-prestressed Reinforcement
  - Constant with time. Obeys Hooke's Law

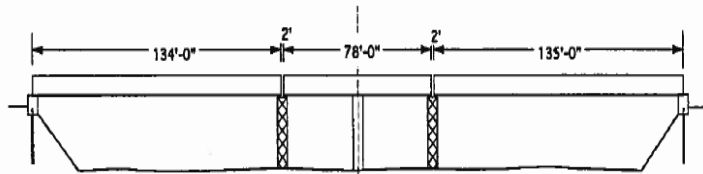


## Timeline Modeling

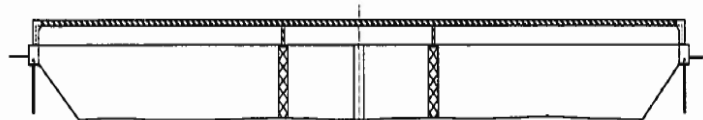


- Modeled as a sequence of discrete intervals
  - Begins when segments are constructed
  - Ends at conclusion of design life
- Interval duration is based on changes in loading and the statical structural system
- Intervals are sub-divided to capture time-dependent material responses immediately following a change in forces

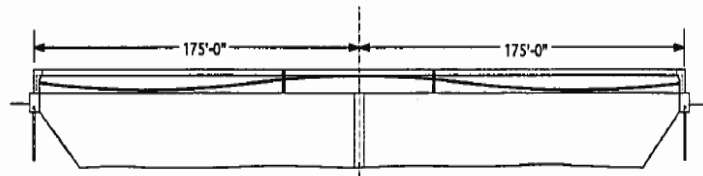
# Typical Timeline



1. Erection of precast girders



2. Form and cast deck, field splices and special end diaphragms



3. Post-tensioning and removal of temporary supports

| Construction Event           | Day of Occurrence |
|------------------------------|-------------------|
| Construct Segments           | 0                 |
| Erect Segments               | 28                |
| Cast Closure Joints and Deck | 35                |
| Install tendons              | 42                |
| Install traffic barrier      | 60                |
| Open to traffic              | 70                |

## Incremental Deformations

- Time-step analysis is simply computing incremental deformations during each interval
- Axial strain and curvature
  - Computed for every part of the girder
  - Caused by
    - externally applied loads
    - change in statical structural system
    - creep and shrinkage of concrete
    - relaxation of prestressing strands and tendons

# Computing Incremental Deformations

$$\Delta \varepsilon_c(i_e, i_b) = \frac{\Delta P_c(i_m)}{A_c E_c(i_m)} [1 + \psi(i_e, i_m)] + \left\{ \sum_{j=1}^{i-1} \frac{\Delta P_c(j_m)}{A_c E_c(j_m)} [\psi(i_e, j_m) - \psi(i_b, j_m)] + \Delta \varepsilon_{sh}(i_e, i_b) \right\}$$

$$\Delta \varphi_c(i_e, i_b) = \frac{\Delta M_c(j_m)}{I_c E_c(j_m)} [1 + \psi(i_e, i_m)] + \left\{ \sum_{j=1}^{i-1} \frac{\Delta M_c(j_m)}{I_c E_c(j_m)} [\psi(i_e, j_m) - \psi(i_e, j_m)] \right\}$$

$$\Delta \varepsilon_{ps}(i_e, i_b) = \frac{\Delta P_{ps}(i_m)}{A_{ps} E_{ps}} + \left\{ -\frac{\Delta f_r(i_e, i_b)}{E_{ps}} \right\}$$

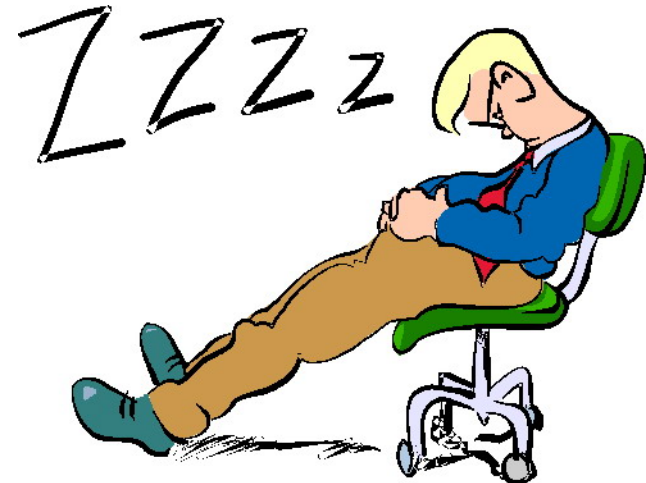
$$\Delta \varepsilon_{ns}(i_e, i_b) = \frac{\Delta P_{ns}(i_m)}{A_{ns} E_{ns}}$$

$$\Delta P_k = \left[ \frac{\Delta P}{A_{tr} E_{tr}} + \frac{\Delta M (Y_{tr} - Y_k)}{I_{tr} E_{tr}} \right] A_k E_k, \quad \Delta M_k = \Delta M \frac{I_k E_k}{I_{tr} E_{tr}}$$

$$\bar{P}_k = -E_k A_k \varepsilon_k, \quad \bar{M}_k = -E_k I_k \varphi_k$$

$$\bar{P} = \sum_{k=1}^n \bar{P}_k, \quad \bar{M} = \sum_{k=1}^n (\bar{M}_k + \bar{P}_k (Y_{tr} - Y_k))$$

$$\bar{\varepsilon} = \frac{\bar{P}}{E_{tr} A_{tr}}, \quad \bar{\varphi} = \frac{\bar{M}}{E_{tr} I_{tr}}$$



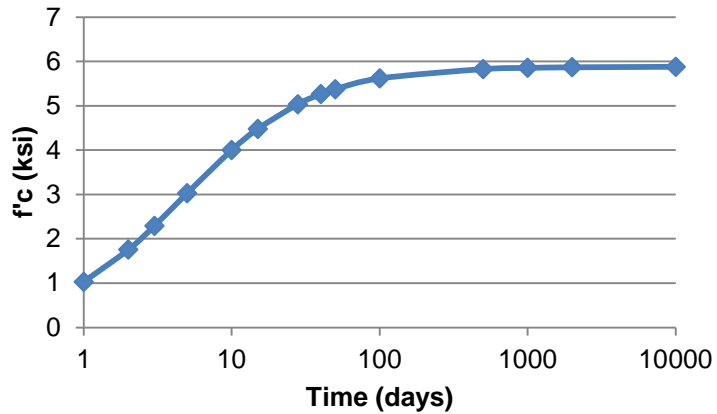
## Time-Step Analysis By Example

- Simple span reinforced concrete beam
- Self-weight loading

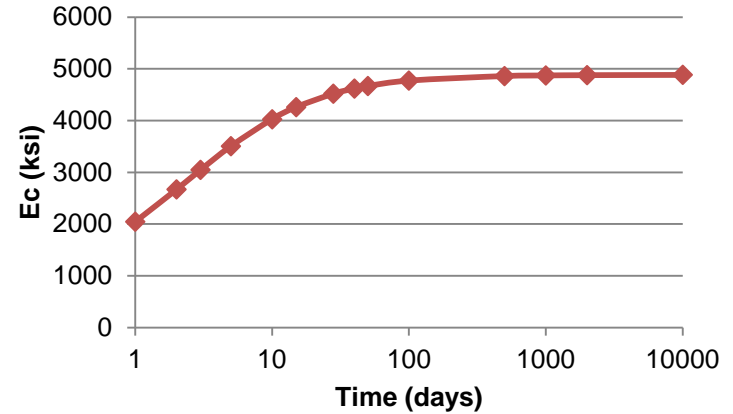


# Time Variation of Material Properties

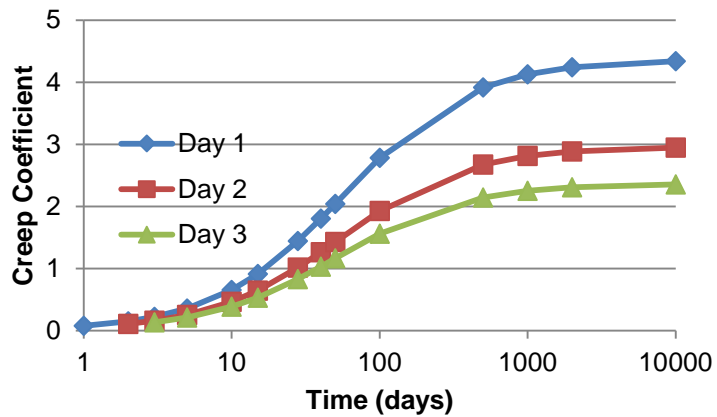
## Time Variation of Concrete Strength



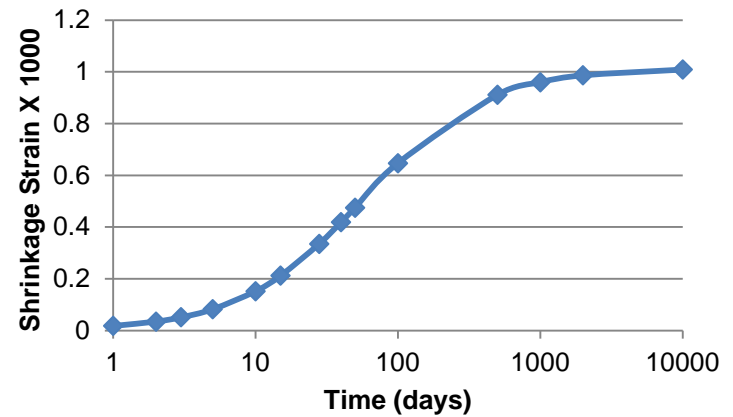
## Time Variation of Concrete Modulus



## Time Variation of Creep Coefficient

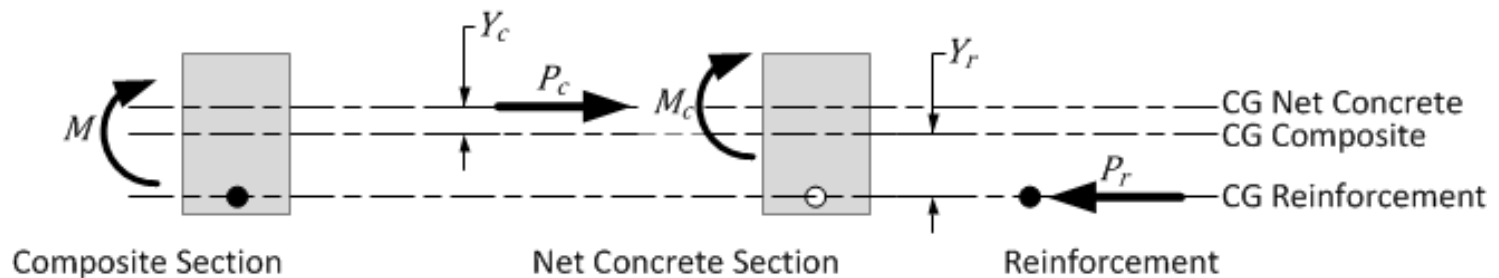


## Time Variation of Shrinkage Strain



## Time Step 1 – Analyze Loading Condition

- Moment due to self-weight (external force)
- Use transformed section analysis
  - Neglect bending stiffness of reinforcement



$$\sum \text{External Forces} = \sum \text{Internal Forces}$$

$$\sum P = 0 = P_c - P_r$$

$$\sum M = M = M_c + P_c Y_c - P_r Y_r$$

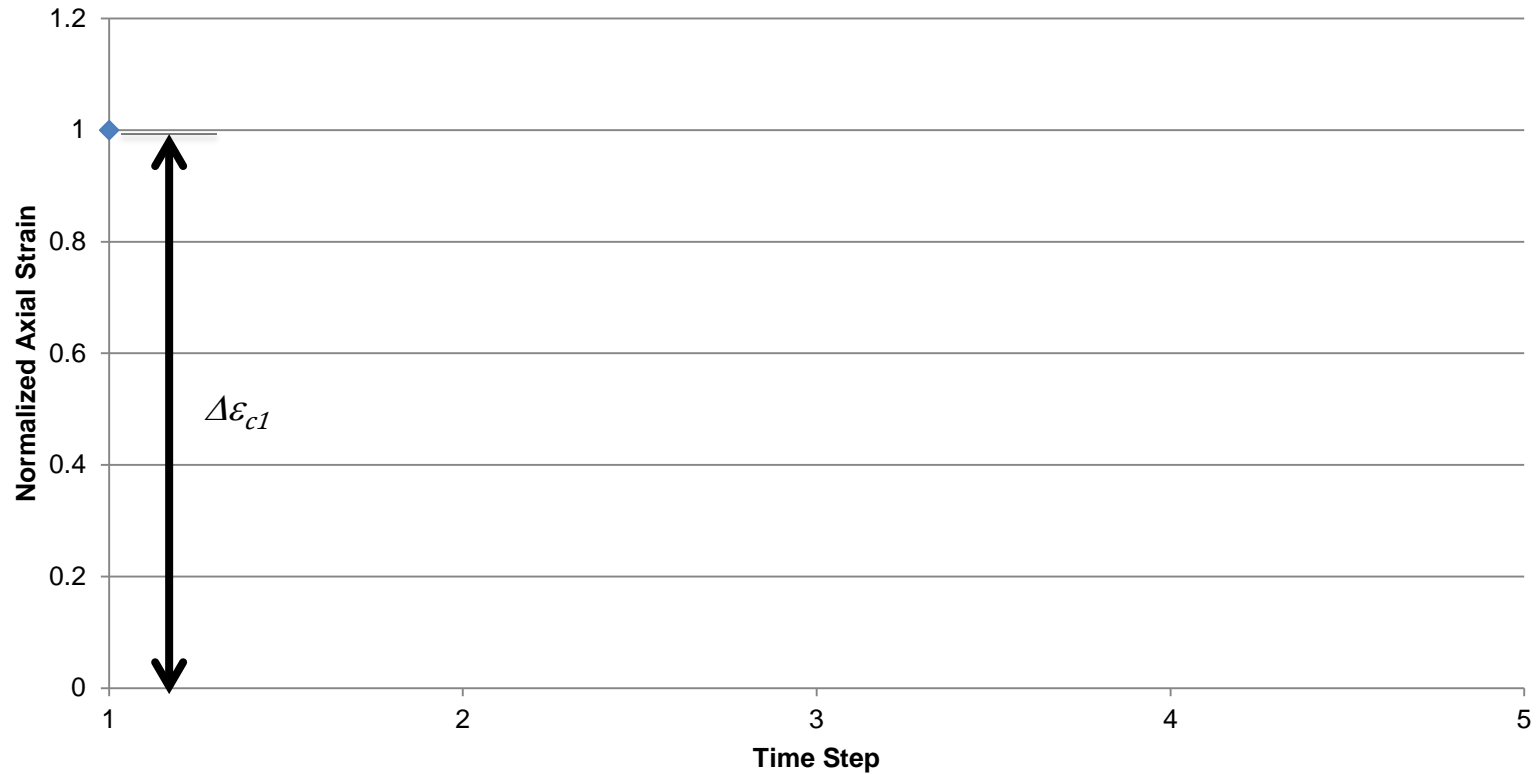
## Time Step 1 – Incremental Deformations

- Incremental forces on the various parts of the cross section are determined by a transformed section analysis
  - $\Delta P_{c1} = P_c, \Delta M_{c1} = M_c, \Delta P_{r1} = P_r$
- Incremental Deformations
  - Computed using modulus at time of loading and net section properties
  - $\Delta \varepsilon_{c1} = \frac{\Delta P_{c1}}{E_{c1} A_{cn}}, \Delta \varphi_{c1} = \frac{\Delta M_{c1}}{E_{c1} I_{cn}}$
  - $\Delta \varepsilon_{r1} = \frac{\Delta P_{r1}}{E_s A_s}$



# Time Step 1 – End of Interval

## Incremental Axial Deformation in Concrete



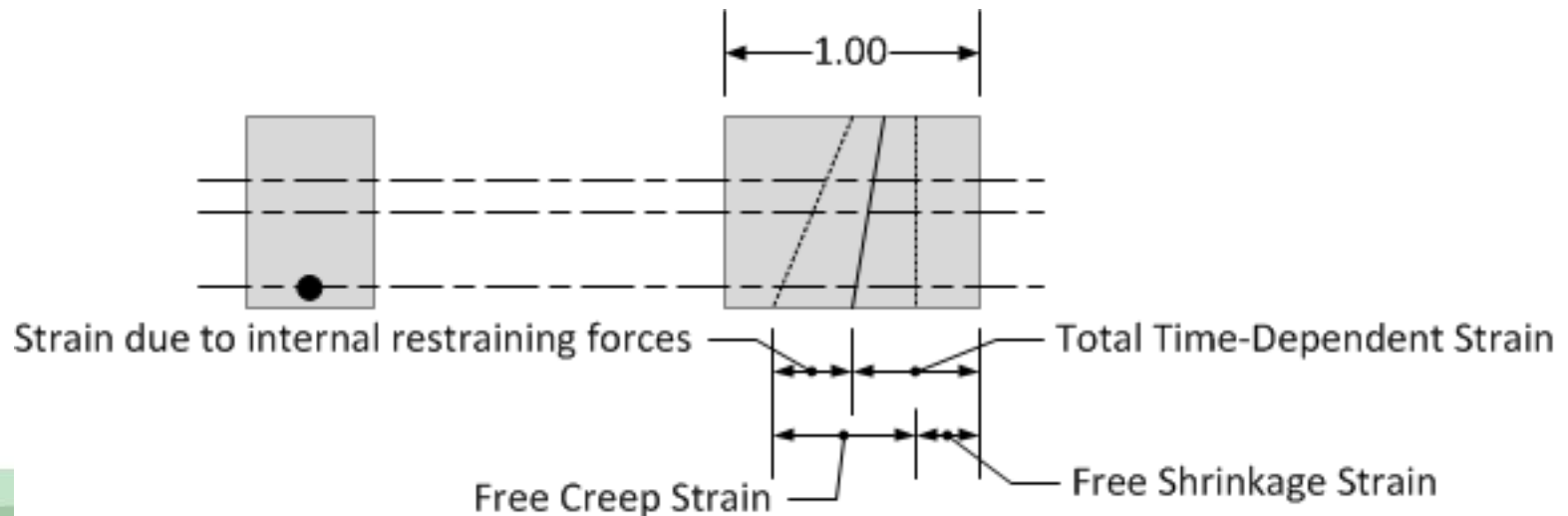
## Time Step 2 – Time-Dependent Effects

- Only Time Passes
- Time-dependent response of materials
  - Unrestrained Creep of Concrete
    - $\Delta\varepsilon_{cr} = \frac{\Delta P_{c1}}{E_1 A_c} \psi(t_2, t_1)$
    - $\Delta\varphi_{cr} = \frac{\Delta M_{c1}}{E_1 I_c} \psi(t_2, t_1)$
  - Unrestrained Shrinkage
    - $\Delta\varepsilon_{sh}(t_2, t_1)$

## Time Step 2 – Initial Strain Analysis

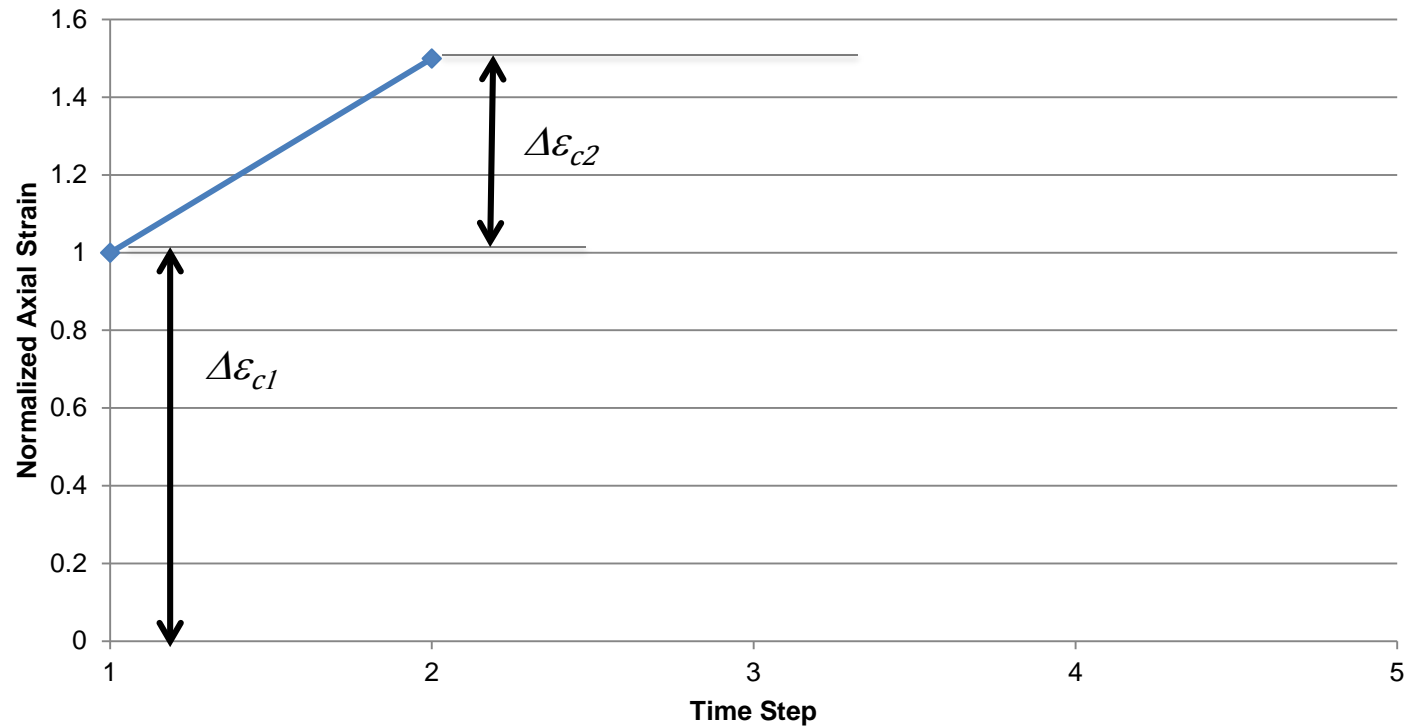
- Reinforcing causing internal restraint
- Compute restrained deformations and internal restraining forces,

$$\Delta\varepsilon_{c2}, \Delta\varphi_{c2}, \Delta\varepsilon_{r2}, \Delta P_{c2}, \Delta M_{c2}, \Delta P_{r2}$$



## Time Step 2 – End of Interval

### Incremental Axial Deformation in Concrete

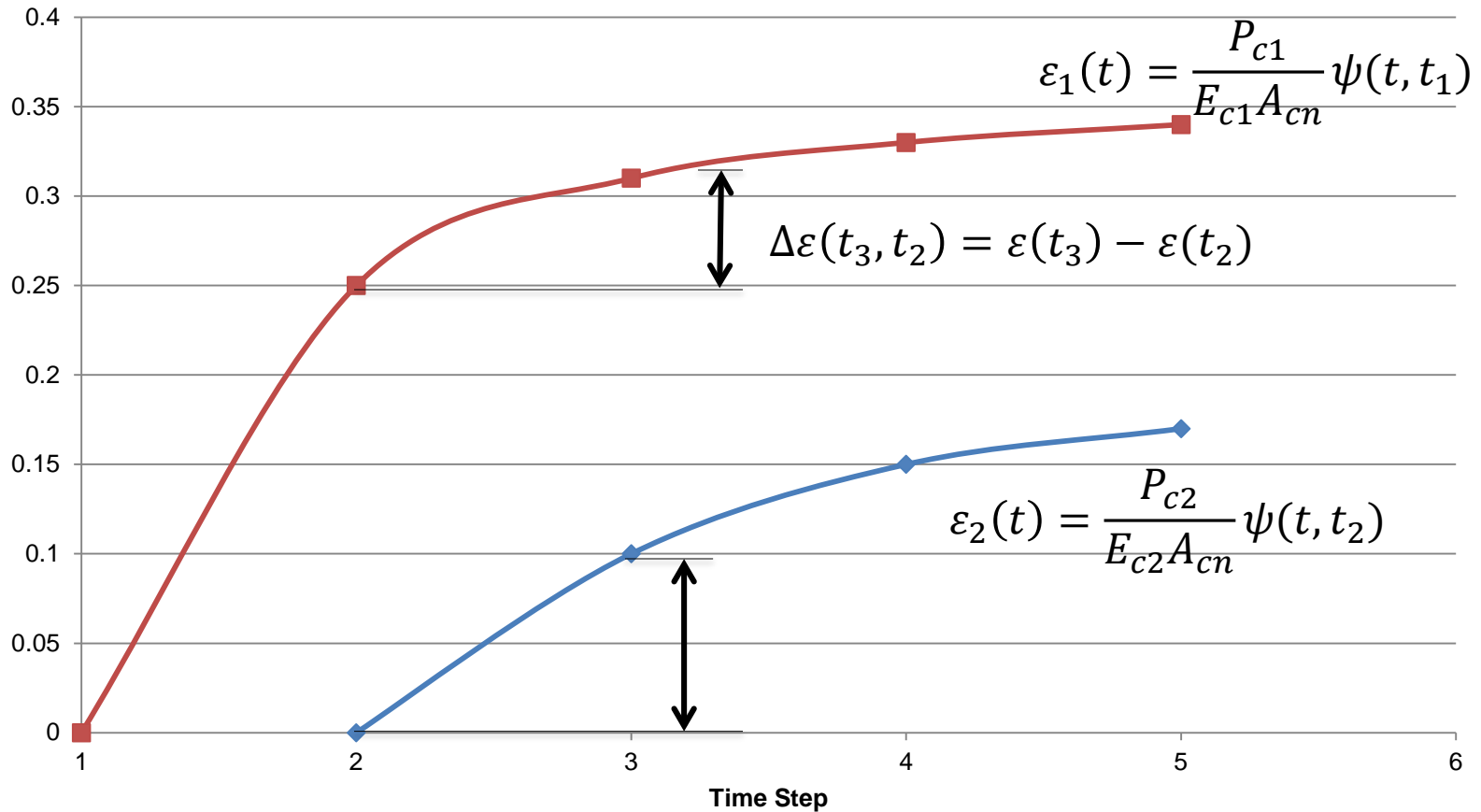


## Time Step 3 – Time-Dependent Effects

- Only Time Passes
- Time-dependent response of materials
  - Unrestrained Creep of Concrete
    - $\Delta\varepsilon_{cr} = \frac{\Delta P_{c1}}{E_1 A_c} [\psi(t_3, t_1) - \psi(t_2, t_1)] + \frac{\Delta P_{c2}}{E_2 A_c} \psi(t_3, t_2)$
    - $\Delta\varphi_{cr} = \frac{\Delta M_{c1}}{E_1 I_c} [\psi(t_3, t_1) - \psi(t_2, t_1)] + \frac{\Delta M_{c2}}{E_2 I_c} \psi(t_3, t_2)$
  - Unrestrained Shrinkage
    - $\Delta\varepsilon_{sh}(t_3, t_2)$

# Time Step 3 – Incremental Unrestrained Deformations

## Unrestrained Axial Creep Strain

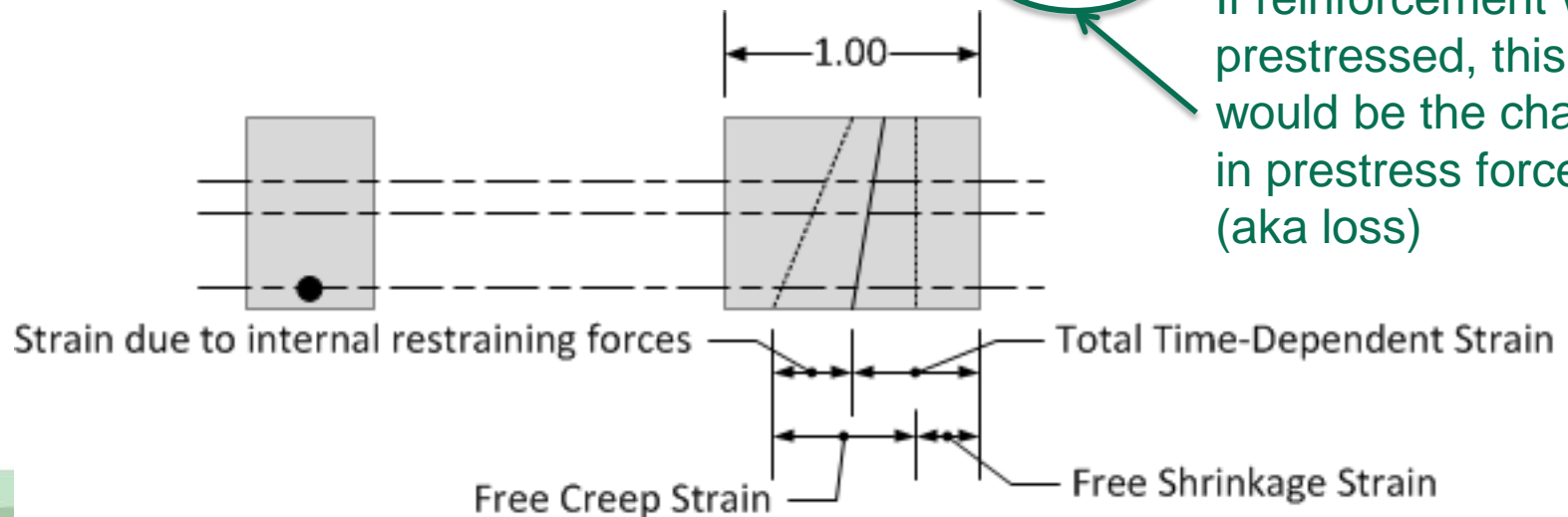


## Time Step 3 – Initial Strain Analysis

- Reinforcing causing internal restraint
- Compute restrained deformations and internal restraining forces,

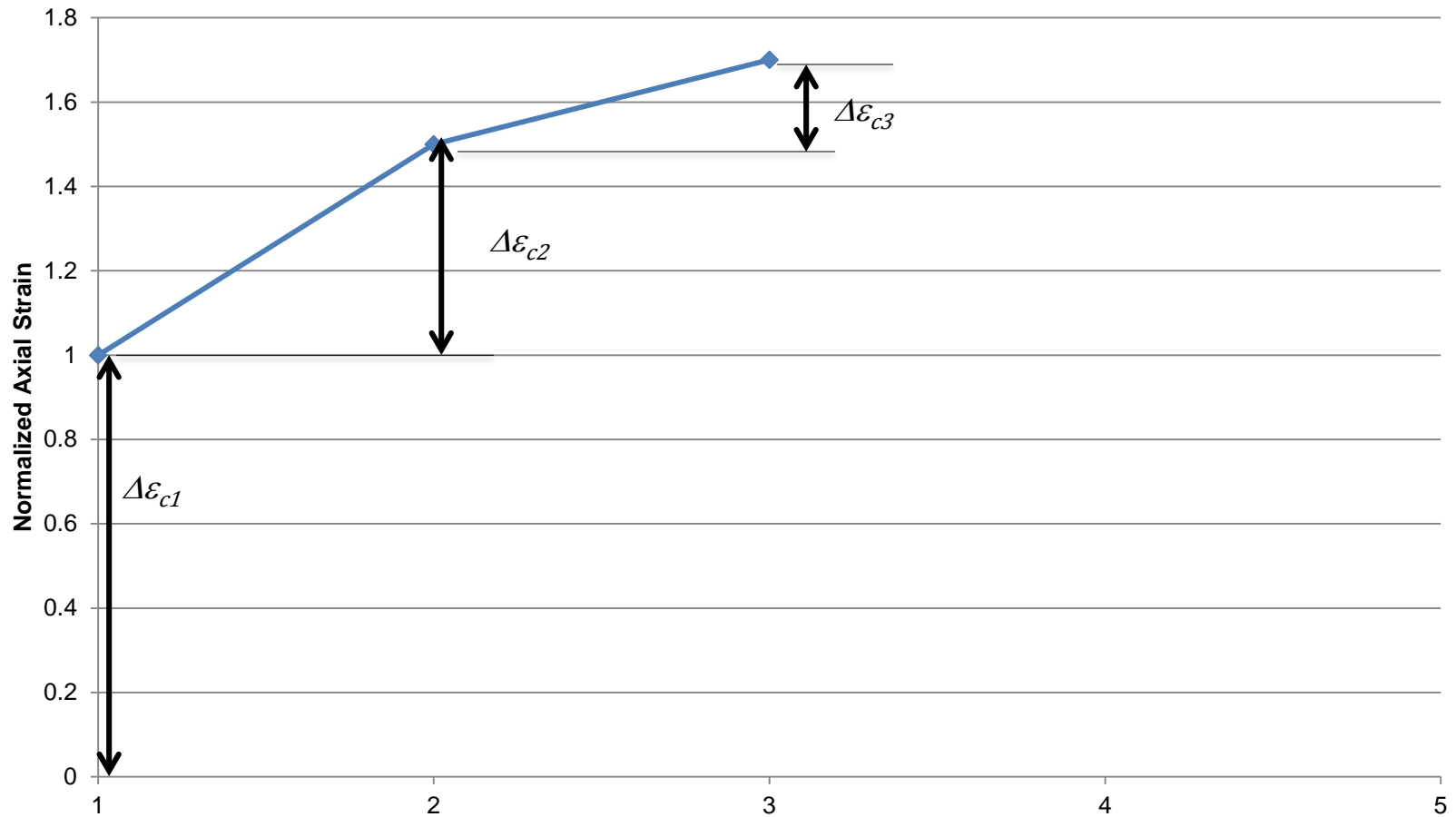
$$\Delta\varepsilon_{c3}, \Delta\varphi_{c3}, \Delta\varepsilon_{r3}, \Delta P_{c3}, \Delta M_{c3}, \Delta P_{r3}$$

If reinforcement were prestressed, this would be the change in prestress force (aka loss)



## Time Step 3 – End of Interval

### Incremental Axial Deformation in Concrete

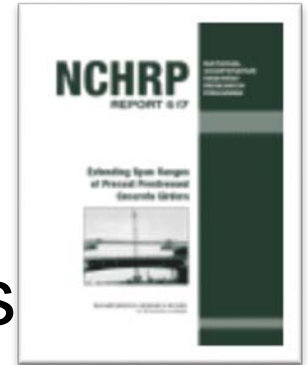




## Time Step $i$ – Repeat, Repeat, Repeat

- This procedure is repeated for every cross section and every time interval
- Analysis is more involved for spliced girders
  - Continuity externally restrains free deformations
  - Several concrete types cast at different times
  - Changes in statical structural system
  - Pretensioning and multi-stage post-tensioning
  - Intrinsic and reduced relaxation of prestressed steel
- Computers are great at performing repetitive computations and keeping track of numbers!

## Computer Aided Design of Spliced Girders



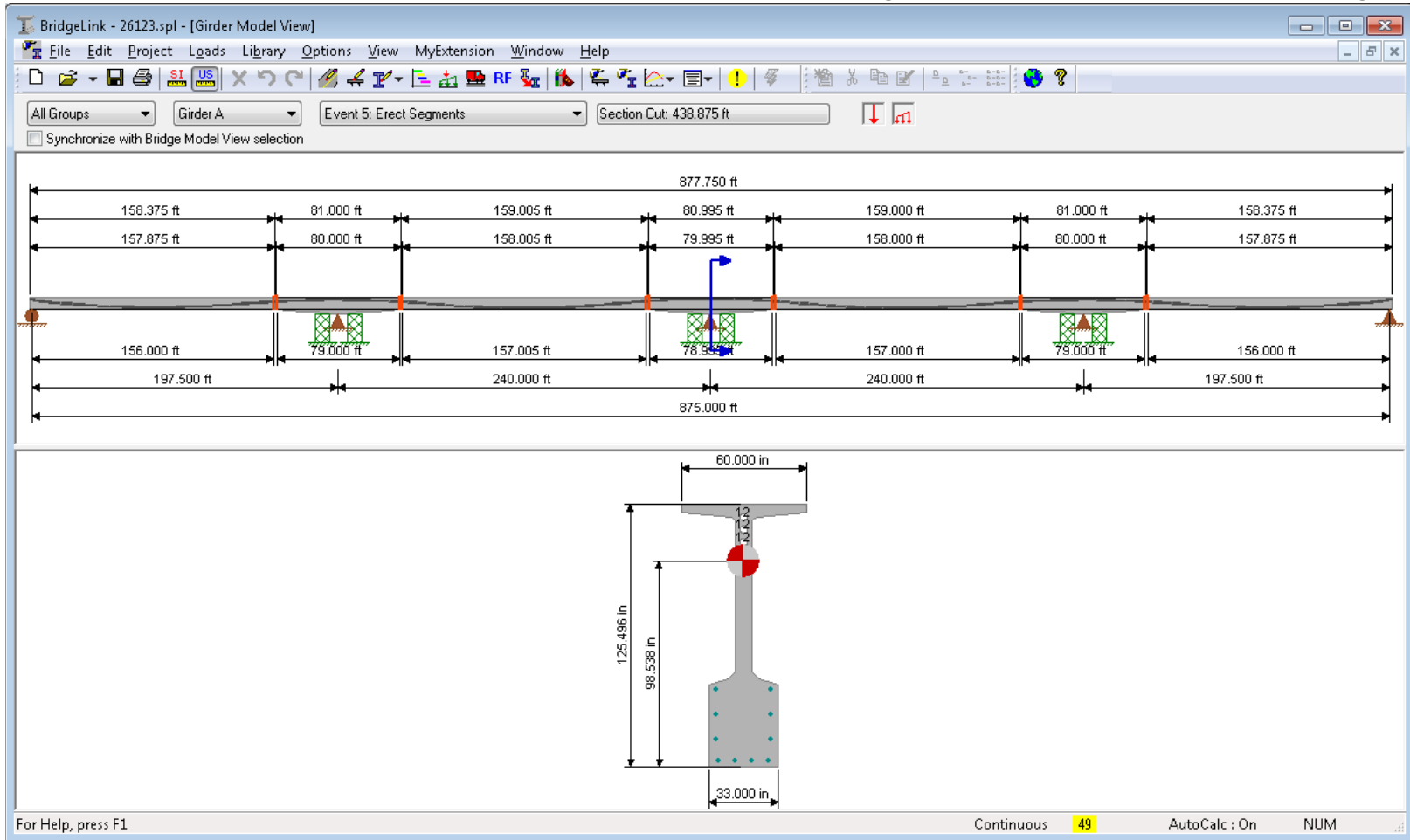
- NCHRP Report 517 – Extending Spans
  - Suggests DOT produced software was a significant contributing factor for wide-spread use of PT Box Girder technology
  - Implies same will be true for adoption of spliced girder technology
  - Notes the lack of a preferred industry standard
  - Recommends owner agencies and industry pursue development of high quality software tools for spliced girder bridges

# PGSplice™

- Part of the new WSDOT BridgeLink™ suite of software
- Design, analyze, and load rate continuous precast-prestressed spliced girder bridges
- Modeling
  - Cantilever pier segments
  - Drop-in field segments
  - Temporary erection towers
  - Strong back hangers
  - Multi-stage post-tensioning
- Analysis
  - Non-linear time step analysis
  - AASHTO, ACI 209 and CEB-FIP Model Code
- User interface, modeling, graphing and reporting features are very similar to PGSuper™

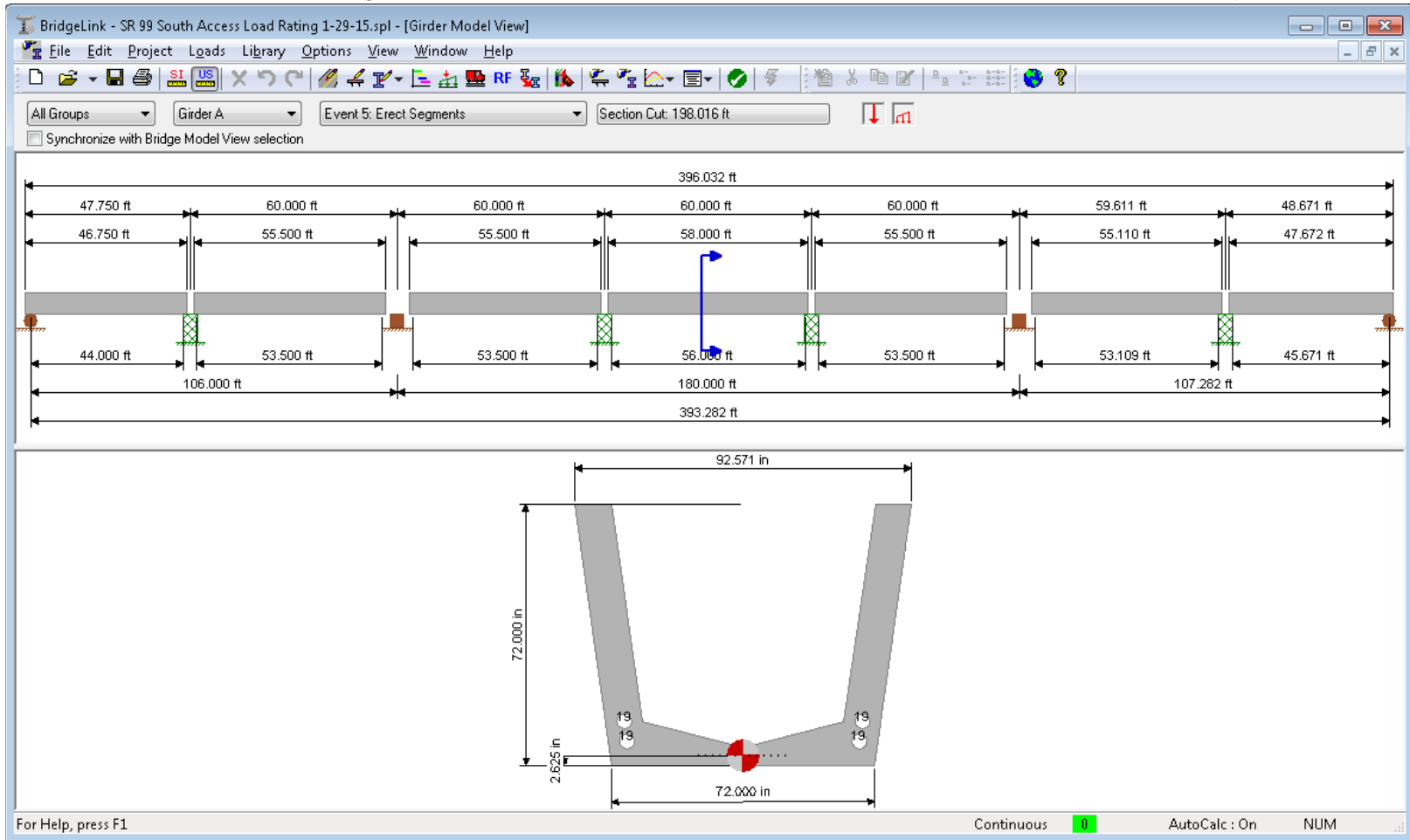
# Bridge Configurations

## 4 Span Variable Depth Girder with Cantilever Piers Segments and Drop In Field Segments



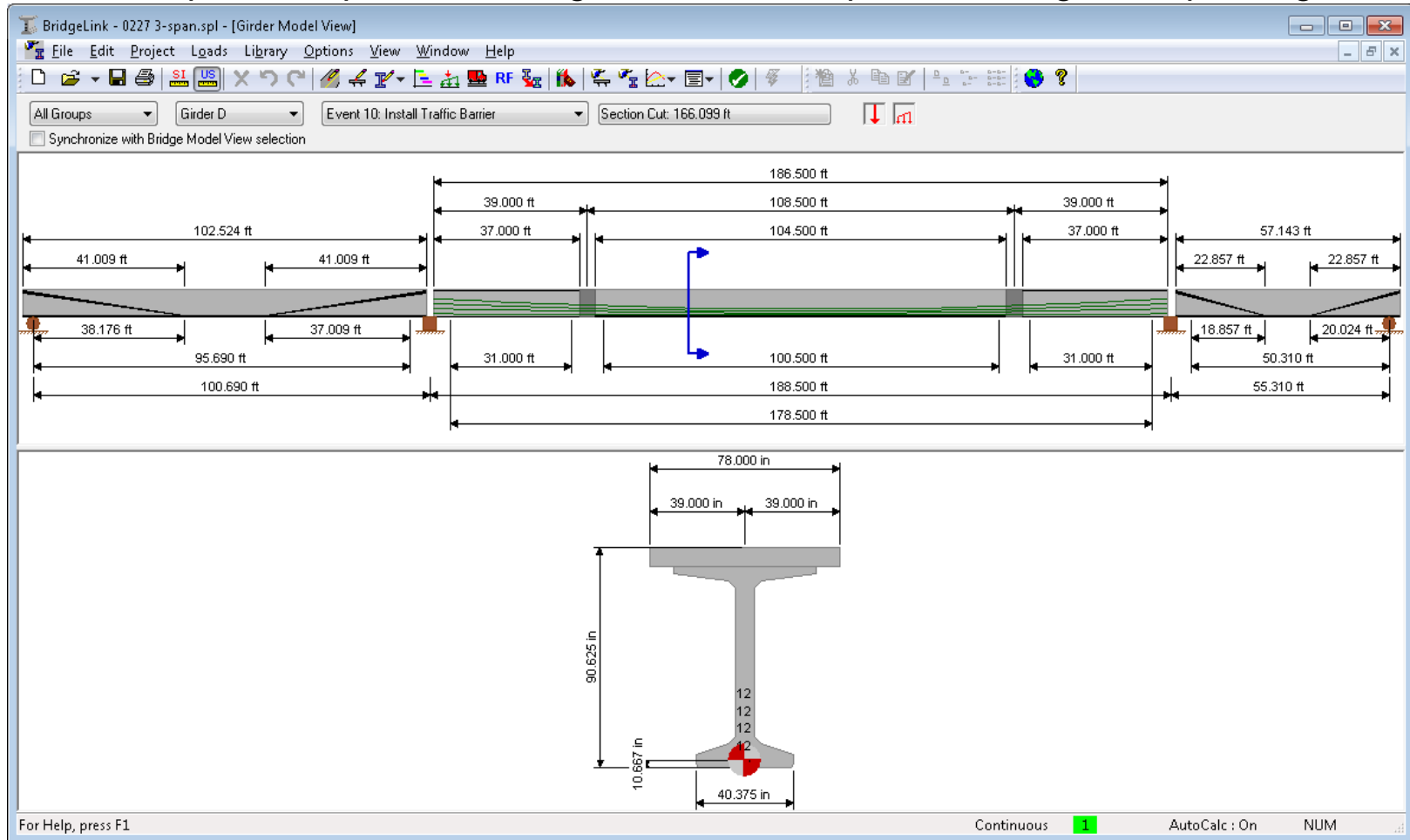
# Bridge Configurations

## 3 Span U-Beam with Segments Supported at Permanent Piers and Temporary Erection Towers



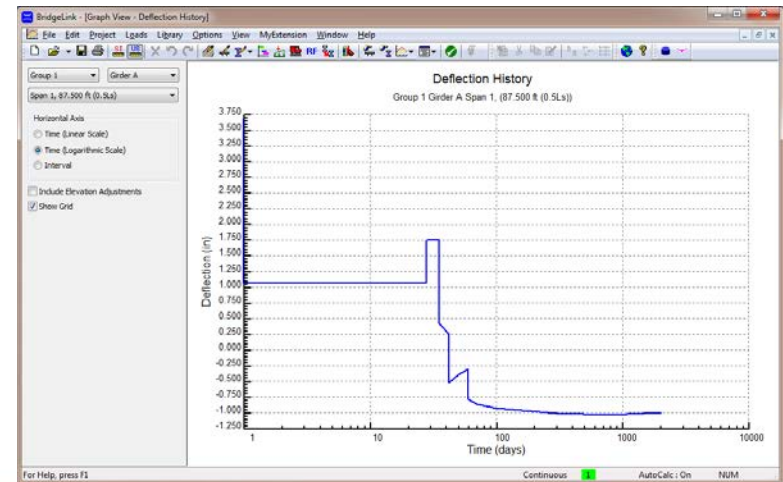
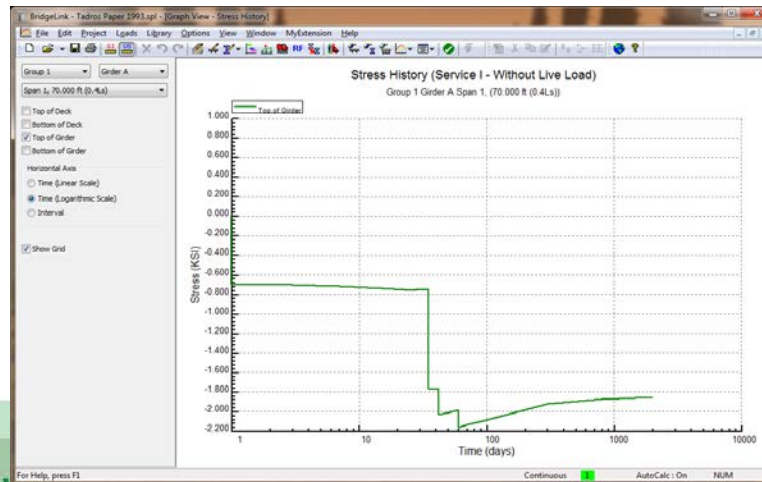
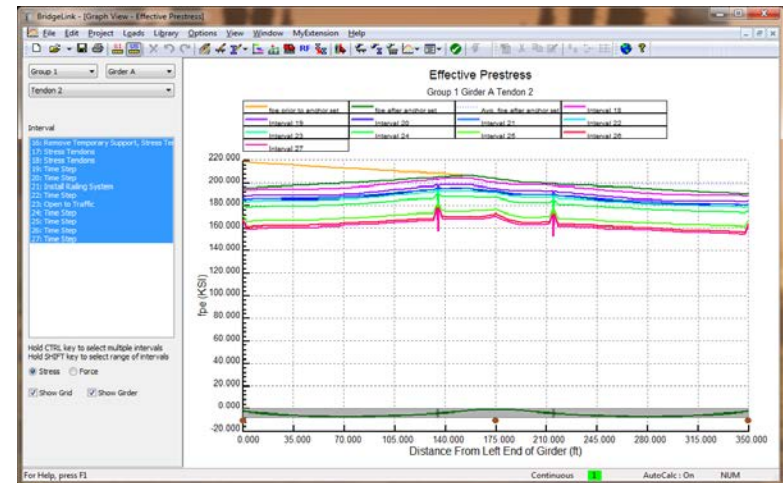
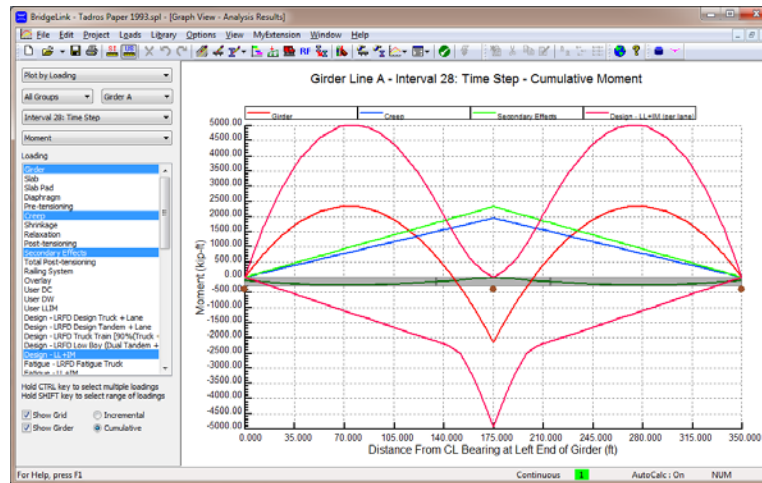
# Bridge Configurations

End Spans are pretensioned girders - center span three segment spliced girder



# Graphical Results

- Visualize Complex Results with Simple Graphical Representations



# Detailed Reporting

- Transparent – eliminate frustration with “black boxes”

BridgeLink - [Time Step Details Report]

File Edit Project Loads Library Options View Window MyExtension Help

Y<sub>k</sub> is measured positive upwards from the top of girder.

**Composite Transformed Section Properties**

$$A_{tr} = \frac{\sum E_k A_k}{E_{tr}} \quad Y_{tr} = \frac{\sum E_k A_k Y_k}{E_{tr} A_{tr}} \quad I_{tr} = \frac{\sum E_k (I_k + A_k (Y_{tr} - Y_k)^2)}{E_{tr}}$$

| Component         | E <sub>tr</sub><br>(KSI) | A <sub>tr</sub><br>(in <sup>2</sup> ) | I <sub>tr</sub><br>(in <sup>4</sup> ) | Y <sub>tr</sub><br>(in) | H<br>(in) |
|-------------------|--------------------------|---------------------------------------|---------------------------------------|-------------------------|-----------|
| Composite Section | 3224                     | 853.775                               | 600285.5                              | -36.172                 | 72.000    |

Y<sub>tr</sub> is measured positive upwards from the top of girder (at the girder/deck interface).

**Unrestrained creep deformation of concrete components due to loads applied in previous intervals**

$$\Delta \epsilon_c(i_a, i_b) = \sum_{j=1}^{i-1} \frac{\Delta P_c(j_m)}{A_c E_c(j_m)} [\psi(i_a, j_m) - \psi(i_b, j_m)]$$

$$\Delta \varphi_c(i_a, i_b) = \sum_{j=1}^{i-1} \frac{\Delta M_c(j_m)}{I_c E_c(j_m)} [\psi(i_a, j_m) - \psi(i_b, j_m)]$$

| Loading Interval | Girder   |  | Deck   |   |
|------------------|--|--|--|---|
|                  | Δε   | Δφ (1/in)  | Δε   | Δφ (1/in)   |
| 1                | (0.00 kip/(0.000 in <sup>2</sup> 2255 KSI))*(1.02212 - 0.769109)=0                   | (0 kip-in/(0.0 in <sup>4</sup> 2255 KSI))*(1.02212 - 0.769109)=0.00000000            | (0.00 kip/(0.000 in <sup>2</sup> 0 KSI))*(0 - 0)=0 | (0 kip-in/(0.0 in <sup>4</sup> 0 KSI))*(0 - 0)=0.00000000 |
| 2                | (-857.41 kip/(813.204 in <sup>2</sup> 2966 KSI))*(0.880683 - 0.634839)=-8.73819e-005 | (-7626 kip-in/(555491.7 in <sup>4</sup> 2966 KSI))*(0.880683 - 0.634839)=-0.00000114 | (0.00 kip/(0.000 in <sup>2</sup> 0 KSI))*(0 - 0)=0 | (0 kip-in/(0.0 in <sup>4</sup> 0 KSI))*(0 - 0)=0.00000000 |
| 3                | (0.00 kip/(813.204 in <sup>2</sup> 2966 KSI))*(0.880683 - 0.634839)=0                | (0 kip-in/(555491.7 in <sup>4</sup> 2966 KSI))*(0.880683 - 0.634839)=0.00000000      | (0.00 kip/(0.000 in <sup>2</sup> 0 KSI))*(0 - 0)=0 | (0 kip-in/(0.0 in <sup>4</sup> 0 KSI))*(0 - 0)=0.00000000 |

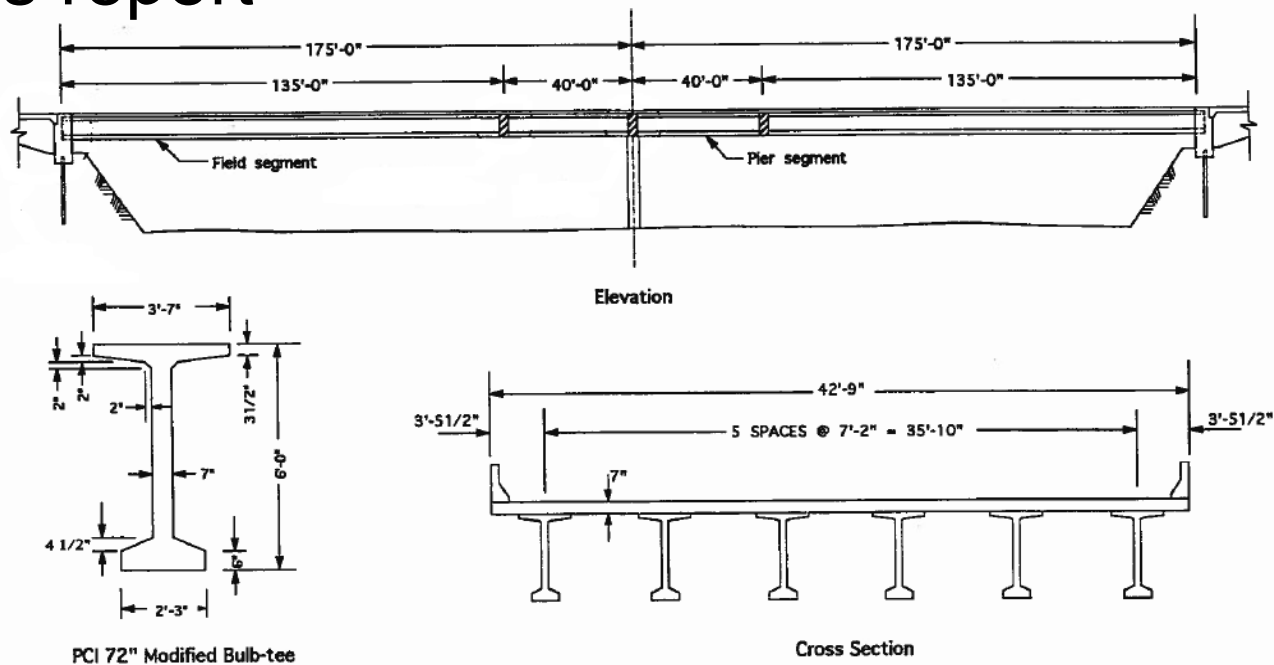
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Continuous **1** AutoCalc: On NUM

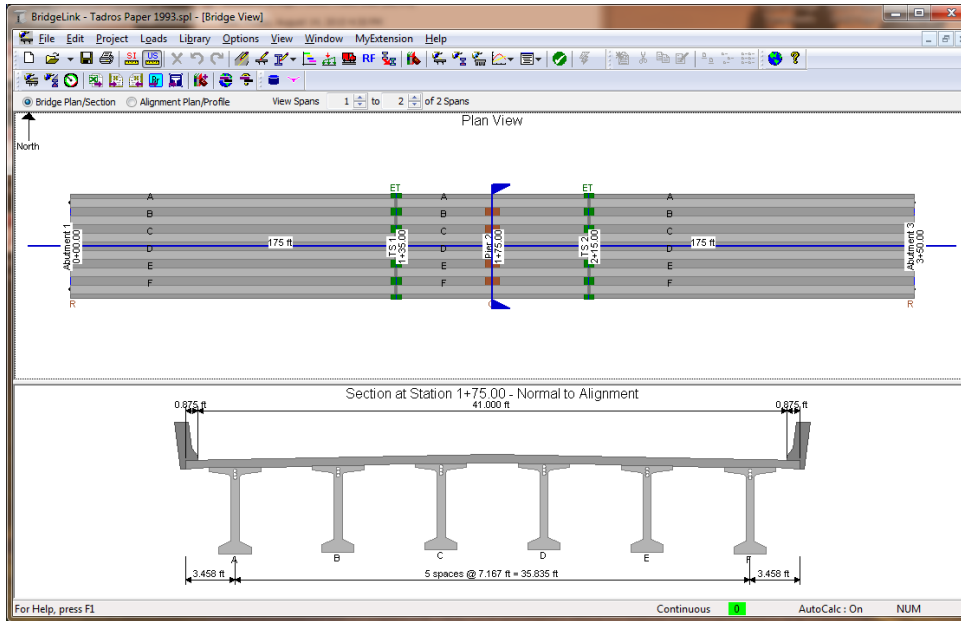


## Case Study

- Two Span Continuous Spliced Girder Bridge
- Presented in PCI State-of-the-Art of Spliced-Girders report



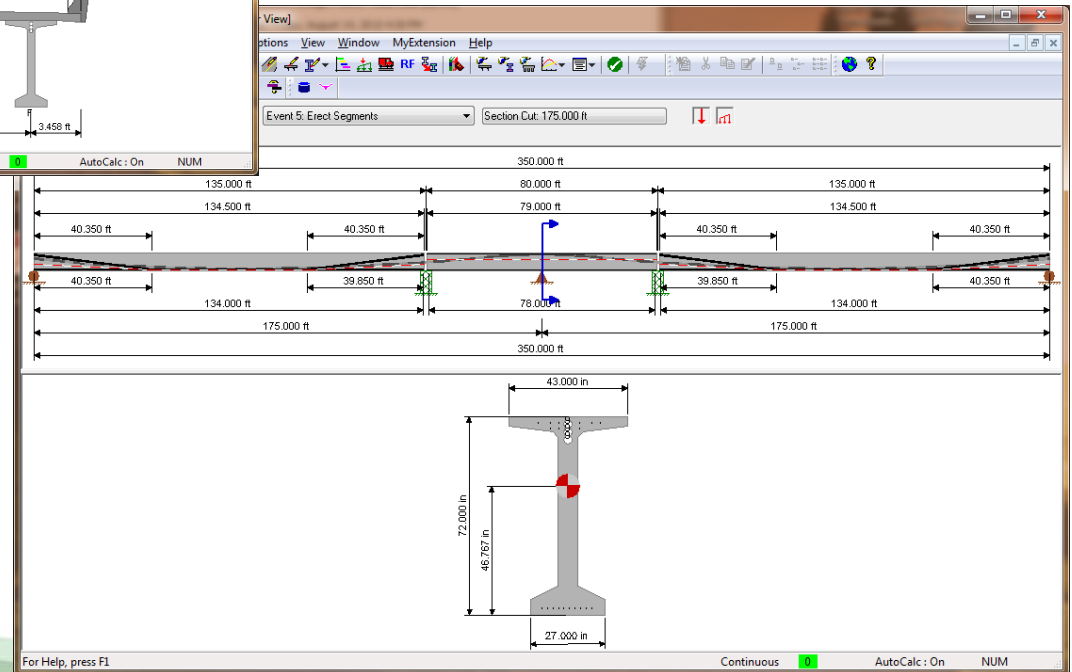
# PGSplice™ Models



Timeline Manager

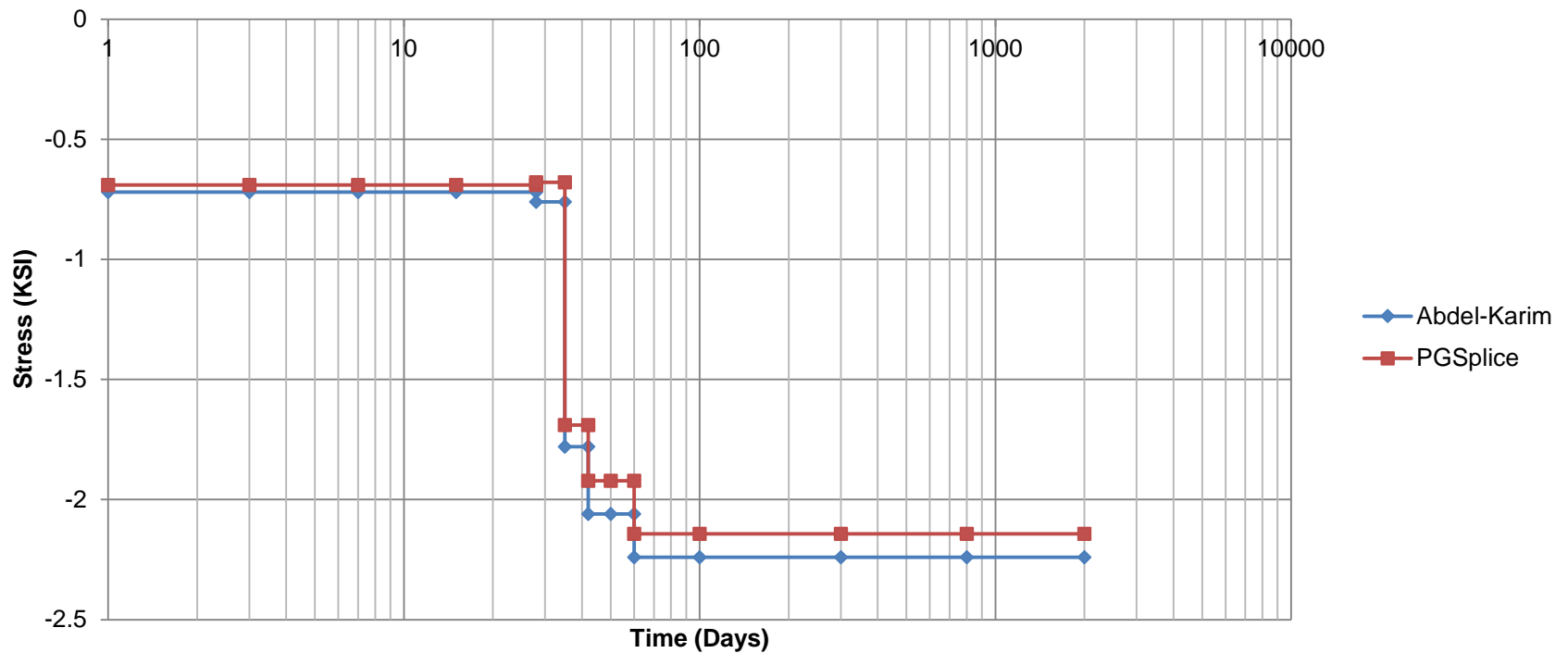
| Event | Occurance (Day) | Elapsed Time (Days) | Description                                   |      |
|-------|-----------------|---------------------|---|------|
| 1     | 0               | 3                   | Construct Segments, Erect Piers               | Edit |
| 2     | 3               | 4                   | Time Step                                     | Edit |
| 3     | 7               | 8                   | Time-Step                                     | Edit |
| 4     | 15              | 13                  | Time-Step                                     | Edit |
| 5     | 28              | 2                   | Erect Segments                                | Edit |
| 6     | 30              | 5                   | Time-Step                                     | Edit |
| 7     | 35              | 7                   | Cast Closures and Deck                        | Edit |
| 8     | 42              | 0                   | Install Tendons and Remove Temporary Supports | Edit |
| 9     | 42              | 0                   | Stress Duct 2                                 | Edit |
| 10    | 42              | 8                   | Stress Duct 3                                 | Edit |
| 11    | 50              | 10                  | Time-Step                                     | Edit |
| 12    | 60              | 10                  | Install Traffic Barrier                       | Edit |
| 13    | 70              | 30                  | Open to Traffic                               | Edit |
| 14    | 100             | 200                 | Time-Step                                     | Edit |
| 15    | 300             | 500                 | Time-Step                                     | Edit |
| 16    | 800             | 1200                | Time-Step                                     | Edit |
| 17    | 2000            |                     | Final time-step                               | Edit |

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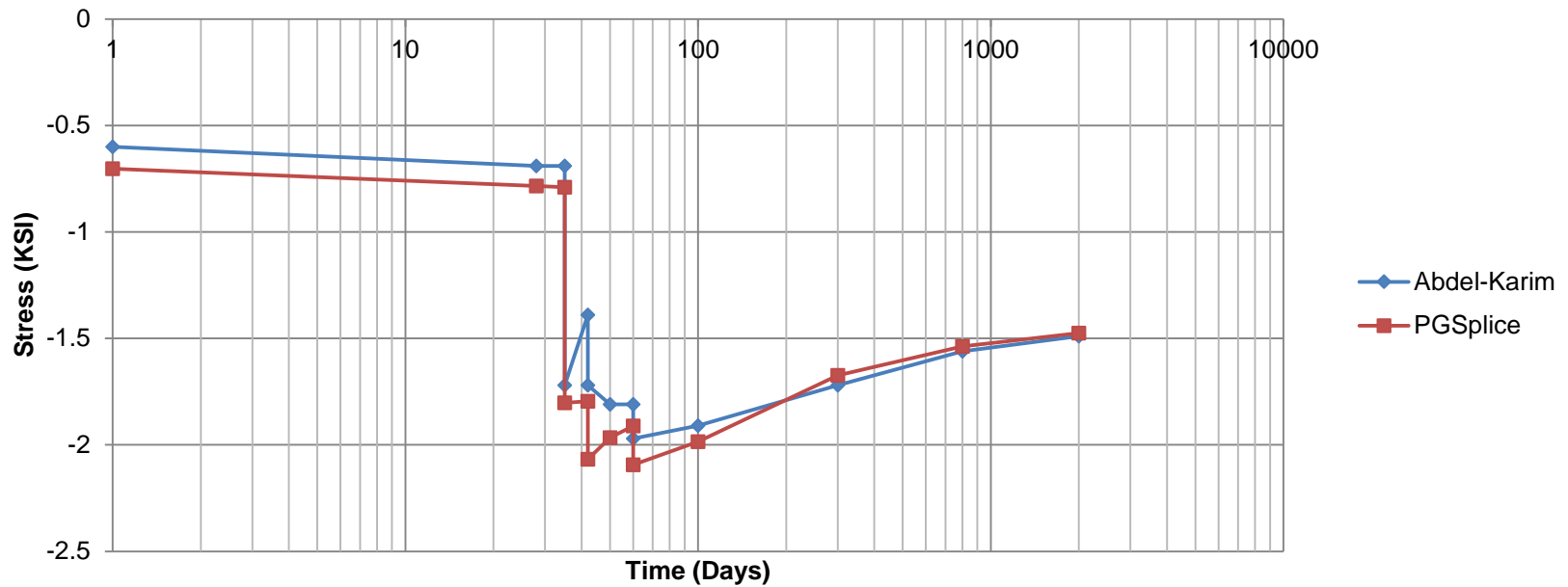
# Baseline Comparison

## Top of Girder Stress at 0.4L in Span 1 without Time Dependent Effects



# Comparison including Time-Dependent Effects

## Top of Girder Stress at 0.4L in Span 1 with Time Dependent Effects



## Software Availability

- Free download from WSDOT
  - <http://www.wsdot.wa.gov/eesc/bridge/software>
- Open Source
- BridgeLink™ v1.0
  - PGSuper™ v3.0 (Beta)
  - PGSplice™ v3.0 (Beta)
  - BEToolbox™ v3.0

<http://www.wsdot.wa.gov/eesc/bridge/software>

