

Probabilistic Damage Control Approach (PDCA) to Seismic Design

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Topics of Discussion

- Introduction
- Background
- Probabilistic Damage Control Approach (PDCA)
- Examples of PDCA
- Next Steps
- Questions

Introduction

Bridge Category (Caltrans MTD 20-1):

- Important
 - Life Safety
 - Major Economic Impact
 - Local Emergency Plan
- Ordinary (SDC)

Introduction, cont.

- Seismic Performance Criteria (*Caltrans*):
 - *Functionality*
 - Ordinary Bridges..... Damage= repairable
 - Important Bridges.....Damage=Minimal
 - *Safety*
 - Ordinary Bridges.....Damage= Significant
 - Important Bridges.....Damage= Repairable



Background

- **Conventional Techniques for Safety and Functionality**
 - Strain Reduction (Reducing ultimate strains of concrete and steel to limit damages)
 - Displacement Ductility Reduction (Reducing target displacement ductility demands to smaller values to limit damages)
- **Proposed Technique**
 - Probabilistic Damage Control Approach (PDCA)

Probabilistic Damage Control Approach (PDCA)



- *Highlights:*

- Acceptable level of damage under each excitation depends on probability of occurrence of the earthquake, that is return period (T) of the earthquake
- Expected Damages at each level of demand can be quantified with Damage Index
- Level of Damage (*Minimal/Repairable/Significant*) can be related to Damage Index

Damage Index

Level of damage in a column at displacement of “ Δ ” is represented by Damage Index (DI):

$$DI = \frac{\Delta_D - \Delta_Y}{\Delta_{UC} - \Delta_Y}$$

DI=0, No damage (Elastic)

DI=1, Extensive Damage (at Collapse)

Damage Index, Cont.

Capacity of columns designed based on current requirements for confinement and other considerations is assumed at $DI \sim 0.5$, however tests have shown columns can withstand larger displacements ($DI \sim 1$)

Design Damage Index (DI) Values

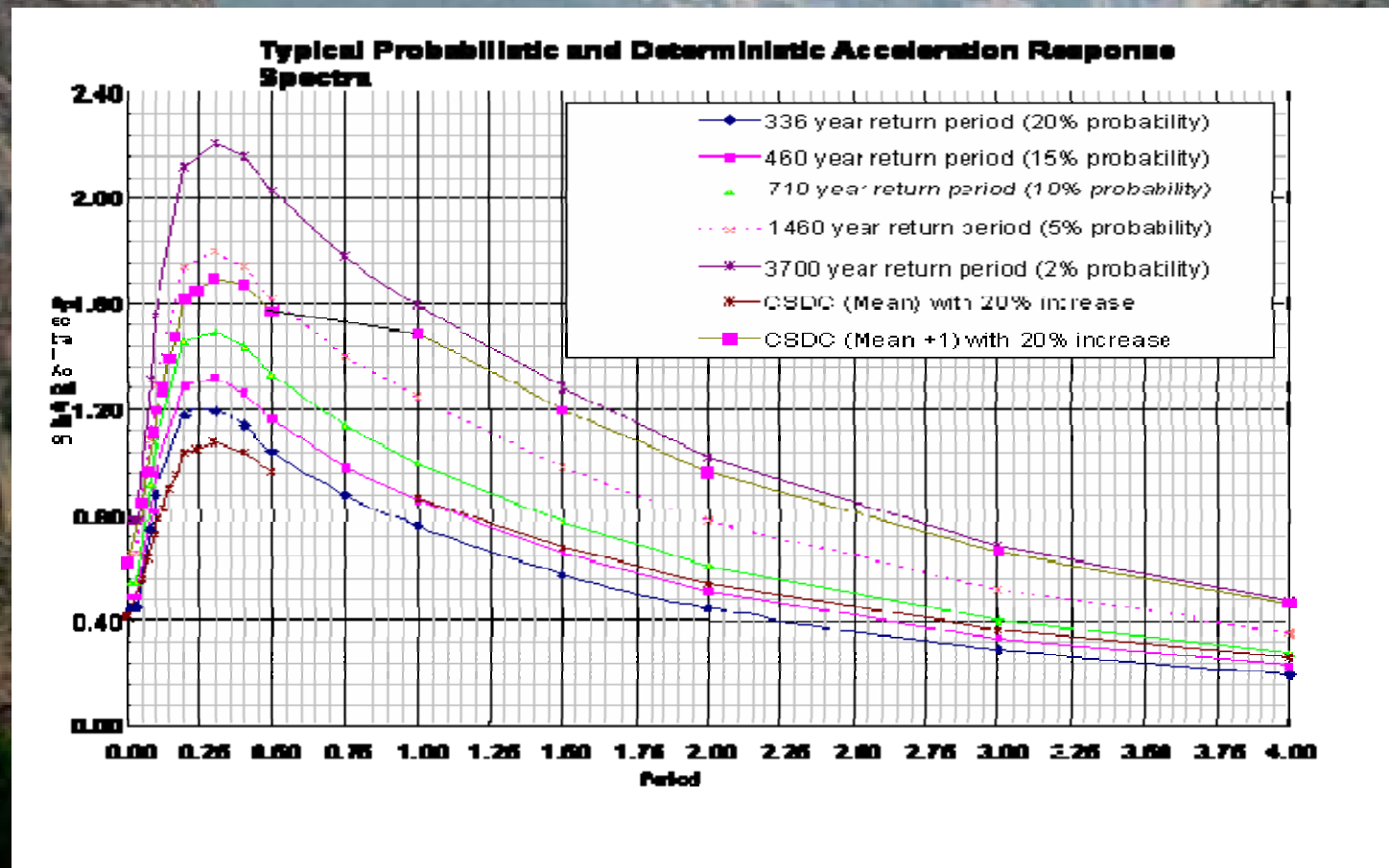
The acceptable level of damage index under each probabilistic ARS curve is design specific, for example it can be:

$T=710$ years* (10% chance of happening in 75 year life): $DI=0.5$

$T=1460$ Years* (5% chance of happening in 75 year life): $DI=0.75$

Note: each of these events are represented by an ARS curve

Typical ARS (75-year exposure time)



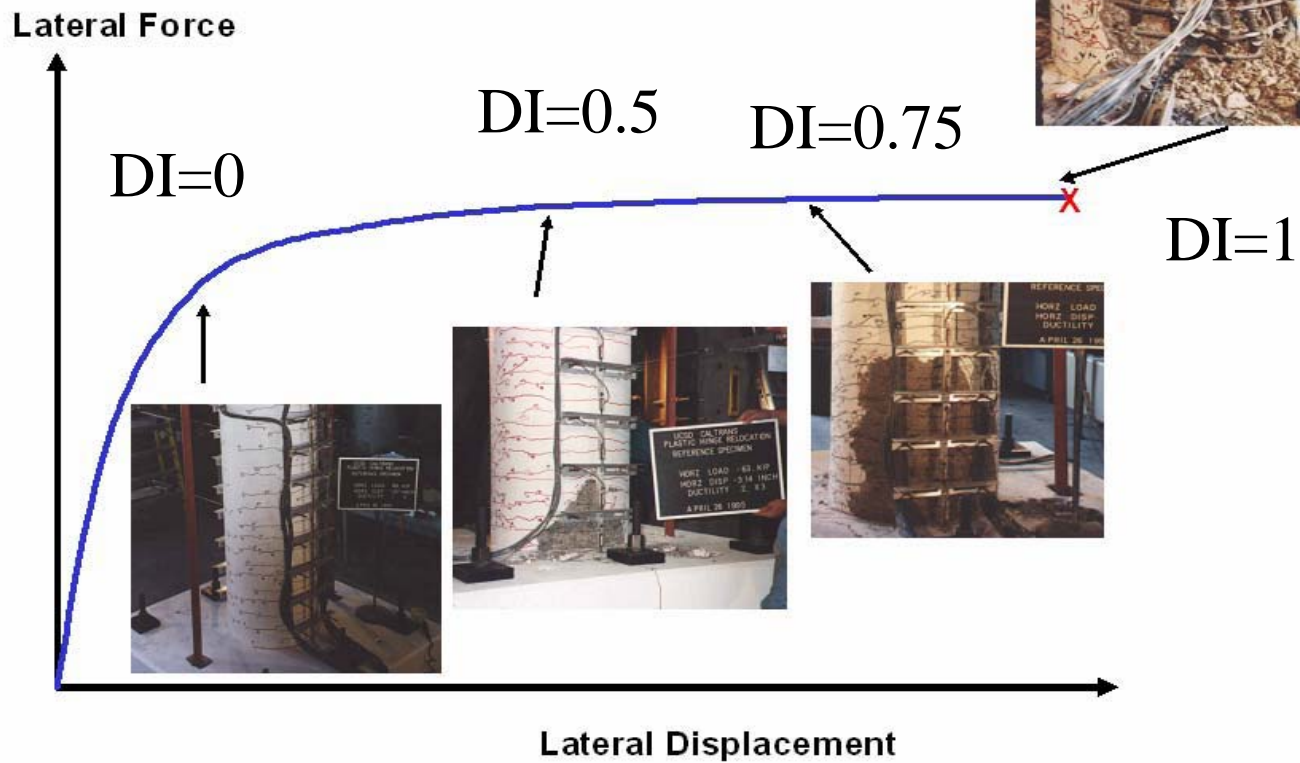
PDCA Design Philosophy

Acceptable level of DI depends on return period of ARS curve used, and SDC requirement of 2-2-4 is modified as:

$$\Delta_D \leq \Delta_Y + DI(\Delta_{UC} - \Delta_Y)$$

Ductile Column Response

Ductile Response (3)



PDCA Advantages

Designer can increase confinement to reduce DI and satisfy design requirements.

Applicable to all parties involved in a project:

Bridge Designers

Bridge Owners (State and Local Agencies)

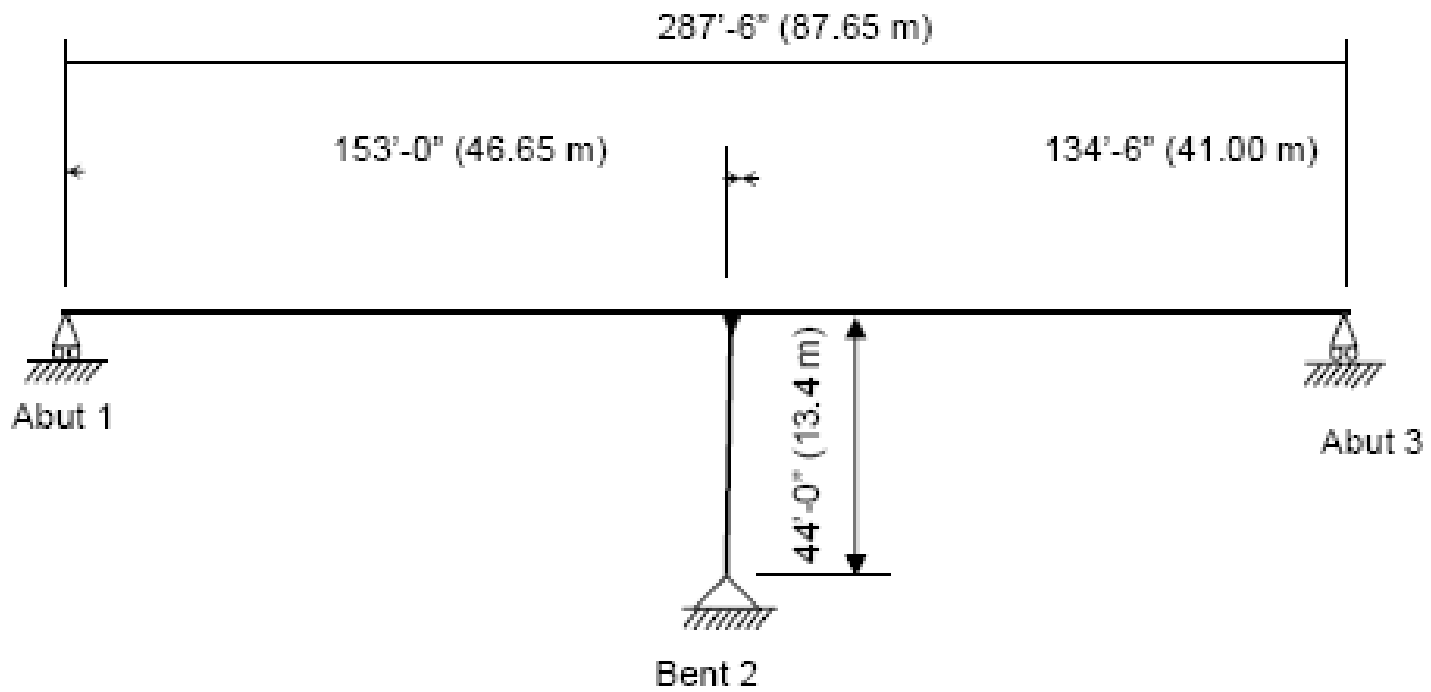
Bridge Maintenance personnel (Repair/retrofit)

Public

EXAMPLES



EXAMPLE # 1



Example # 1

- The superstructure of the bridge consists of a six-cell post-tensioned box girder supported on drilled pile-shaft
- Caltrans' site specific deterministic ARS curve and also a family of probabilistic ARS curves are used.
- The performance push-over (transverse analysis) indicates that two plastic hinges form at top of columns.
- Comparison of ultimate displacement capacity (Δ_{uc}) and demand (D_D) shows adequate ductility in the transverse direction for this particular bent.
- The plastic component of the displacement capacity is based on an effective length of column defined from the Contraflexure point or zero moment to the center the upper plastic hinge.

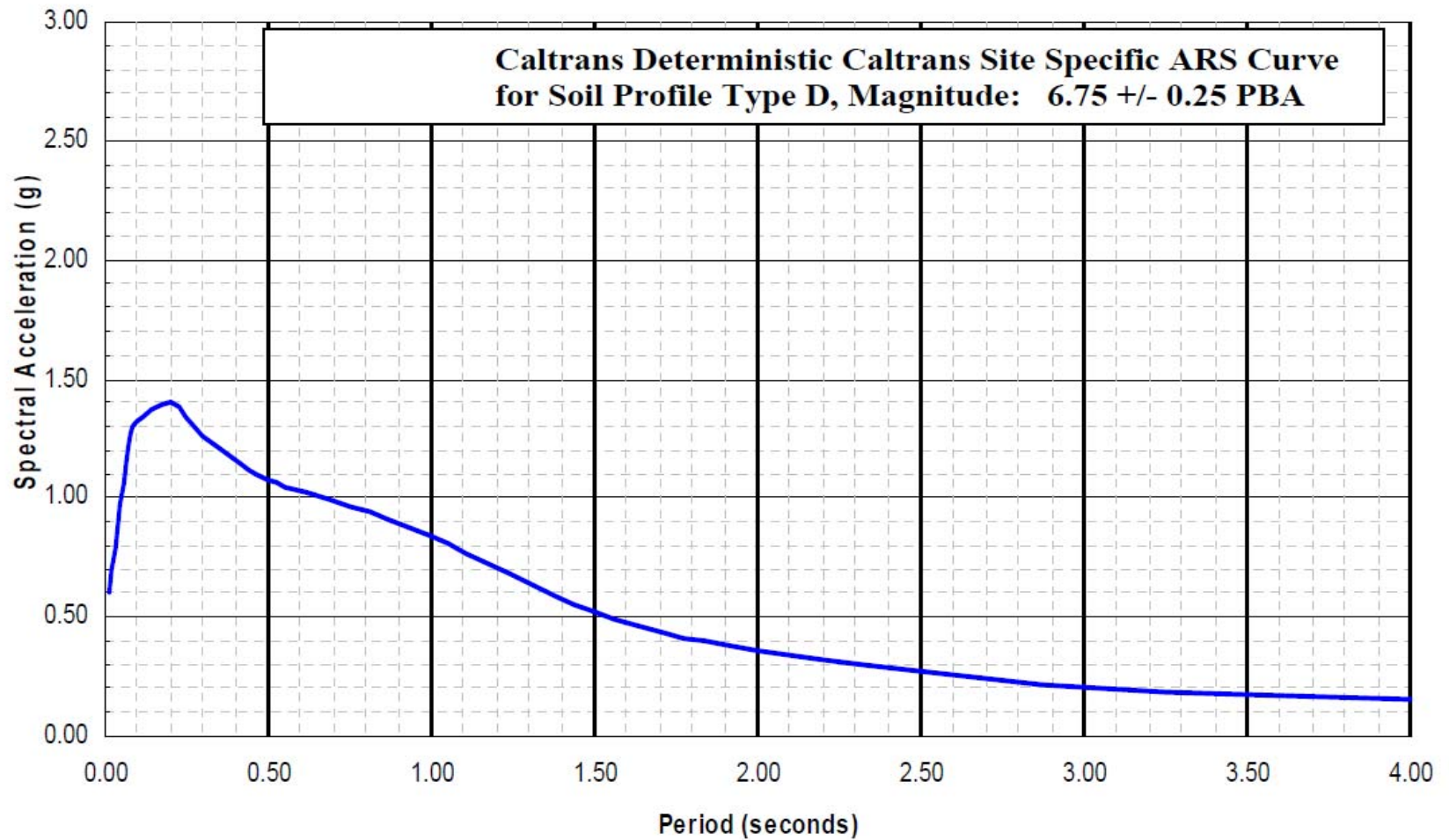
EXAMPLE # 1

- The longitudinal bars in the column consists of 36 No. 11 bars, the confinement consists of No. 8 hoops @ 4 inches spacing in the plastic hinge region. The plastic moment and curvature were calculated using sectional fiber analysis software
- The over-turning effects increased the axial load from 2034 kips to 2911 kips in the compression column; however, the increase in plastic moment was only 8.4%. There is additional reserved capacity in the cap beam to easily meet the higher column moments.

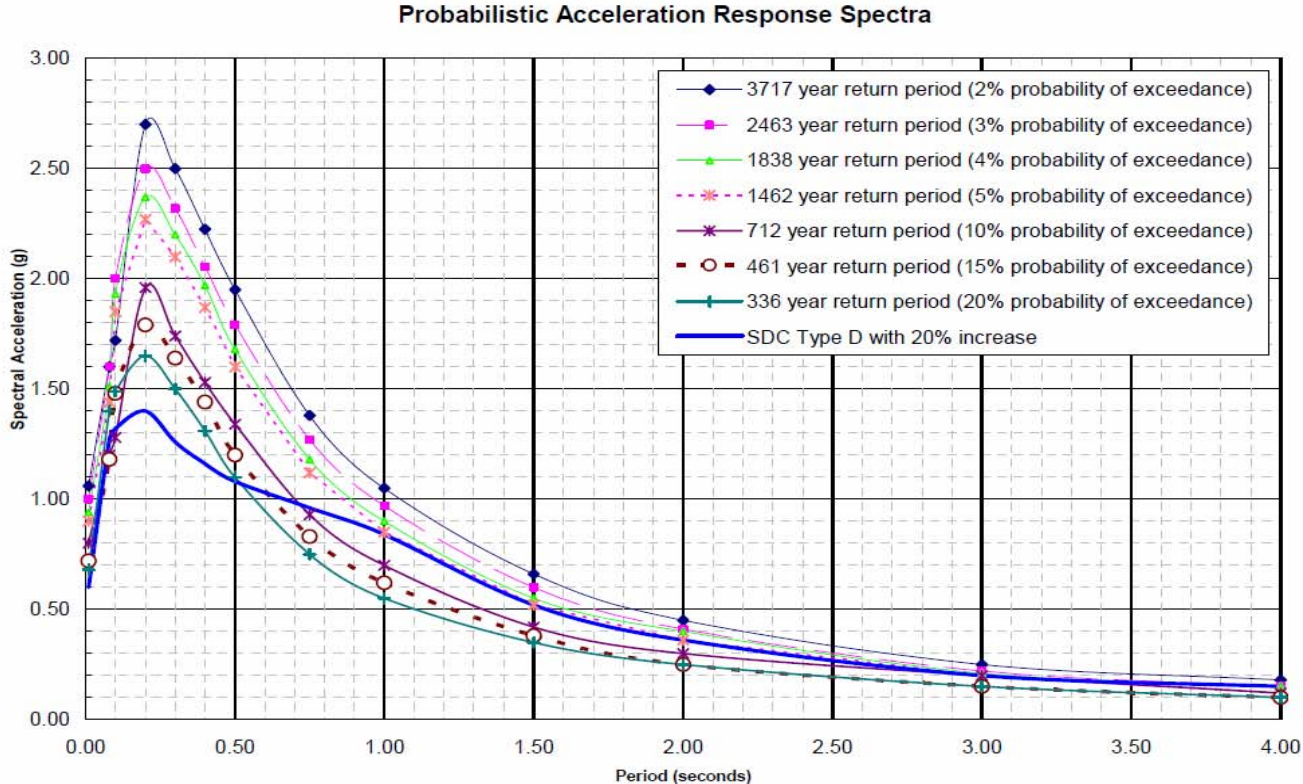
COLUMN PROPERTIES PDCA

| D | P | M _p | ε _{cu} | Φ _p | I _{cr} | E _c | f' _c |
|---------------|--------|----------------|-----------------|----------------|--------------------|----------------|-----------------|
| | (kips) | (K-ft) | | (rad/in) | (ft ⁴) | (ksf) | (ksi) |
| 5.5 ft Circle | 2034 | 12935 | 0.0348 | 0.00187 | 19.98 | 580000 | 5 |

EXAMPLE # 1

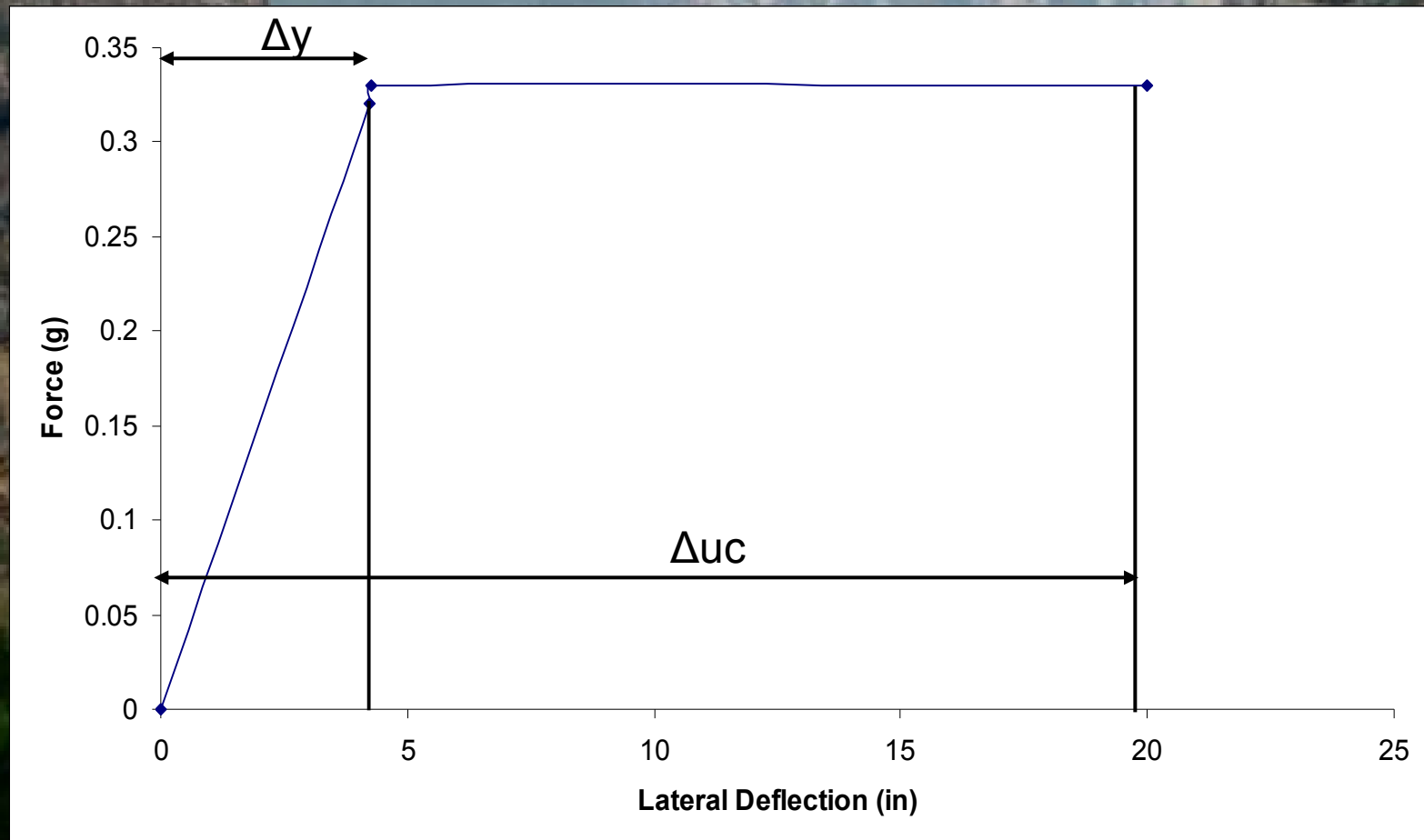


EXAMPLE # 1



EXAMPLE # 1

Transverse Push-Over Analysis



EXAMPLE # 1

Safety Evaluation:

The bridge is evaluated for safety when exposed to deterministic design earthquake. Following is summary of displacement demand and capacity calculations for safety evaluation of Bent 2.

$$k_i = \text{initial slope} = \frac{\text{Lateral Force}}{\text{Yield Displacement}} = \frac{0.32W}{\Delta_y} = \frac{0.32 \times 4064 \text{ kips}}{4.22"} = 308.4 \text{ k/in}$$

$$T = 0.32 \sqrt{\frac{W}{k_i}} = 0.32 \sqrt{\frac{4064}{308.4}} = 1.16 \text{ seconds}$$

From CSDC (Mean) ARS curve is calculated as 0.75g.

$$\Delta_D = \frac{F}{k_i} = \frac{0.75 \times 4064}{308.4} = 9.90 \text{ inches}$$

$$\Delta_{UC} = \Delta_p + \Delta_y \text{ for the plastic hinge}$$

$$l_p = \text{Length of plastic hinge} = 0.08L_1 + 10.2d_b$$

$$l_p = 0.08 \times 20 \times 12 + 10.2 \times 1.63 = 35.83"$$

$\theta_p = l_p \phi_p$, and l_p is the plastic curvature capacity at top of column from sectional analysis.

$$\theta_p = 35.83" \times 0.00187 = 0.0670 \text{ radians}$$

$$\Delta_p = \theta_p * (L_1 - l_p/2) = 0.0670 \times (20 \text{ ft} (12) - 35.83" / 2) = 14.88"$$

$$\Delta_{UC} = 14.88 + 4.22 = 19.10" > \Delta_D = 9.90" \therefore \text{OK}$$

Damage Index

$$DI = \frac{\Delta_D - \Delta_y}{\Delta_{UC} - \Delta_y} = \frac{9.90 - 4.22}{19.10 - 4.22} = 0.38 < 0.5 \therefore \text{OK}$$

EXAMPLE # 1

Functionality Evaluation:

The bridge is evaluated for functionality when exposed to the family of probabilistic ARS curves. The Bent # 2 sample calculations of displacement demand and capacity for probabilistic ARS Curve with 10% probability of exceedance is summarized as:

$$k_i = \text{initial slope} = \frac{\text{Lateral Force}}{\text{Yield Displacement}} = \frac{0.32g}{\Delta_y} = \frac{0.32 \times 4067 \text{ kips}}{4.22"} = 308.4 \text{ k/in}$$

$$T = 0.32 \sqrt{\frac{W}{k_i}} = 0.32 \sqrt{\frac{4067}{308.4}} = 1.16 \text{ seconds}$$

From 10% ARS Curve spectral acceleration is calculated as 0.60g.

$$\Delta_D = \frac{F}{k_i} = \frac{0.60 \times 4064}{308.4} = 7.91 \text{ inches}$$

Similarly, $\Delta_{UC} = \Delta_P + \Delta_y$

$$\Delta_{UC} = 14.88 + 4.22 = 19.10" > \Delta_D = 7.91" \therefore \text{OK}$$

Damage Index

$$DI = \frac{\Delta_D - \Delta_y}{\Delta_{UC} - \Delta_y} = \frac{7.91 - 4.22}{19.10 - 4.22} = 0.25$$

EXAMPLE # 1

DAMAGE INDEX

| Column | Δ_p | Δ_y | T | a (ARS) | Δ_D | Δ_{uc} | Damage | Acceptable | Comment |
|------------------------|------------|------------|------|---------|------------|---------------|--------|-------------|---------|
| Code | (in) | (in) | sec | (g) | (in) | (in) | DI | DI (2 Cols) | Good/NG |
| Caltrans Type D (0.5g) | 14.88 | 4.22 | 1.16 | 0.47 | 9.90 | 19.10 | 0.38 | 0.6 | Good |
| Example Bridge 20% | 14.88 | 4.22 | 1.16 | 0.30 | 6.26 | 19.10 | 0.14 | 0.3 | Good |
| Example Bridge 15% | 14.88 | 4.22 | 1.16 | 0.33 | 7.25 | 19.10 | 0.20 | 0.4 | Good |
| Example Bridge 10% | 14.88 | 4.22 | 1.16 | 0.38 | 7.91 | 19.10 | 0.25 | 0.5 | Good |
| Example Bridge 5% | 14.88 | 4.22 | 1.16 | 0.48 | 9.90 | 19.10 | 0.38 | 0.8 | Good |
| Example Bridge 4% | 14.88 | 4.22 | 1.16 | 0.49 | 10.28 | 19.10 | 0.41 | 0.9 | Good |
| Example Bridge 3% | 14.88 | 4.22 | 1.16 | 0.53 | 11.08 | 19.10 | 0.46 | 1 | Good |
| Example Bridge 2% | 14.88 | 4.22 | 1.16 | 0.58 | 12.13 | 19.10 | 0.53 | 1 | Good |

Therefore, the bridge complies with limits proposed for DI values under different probabilistic excitations.

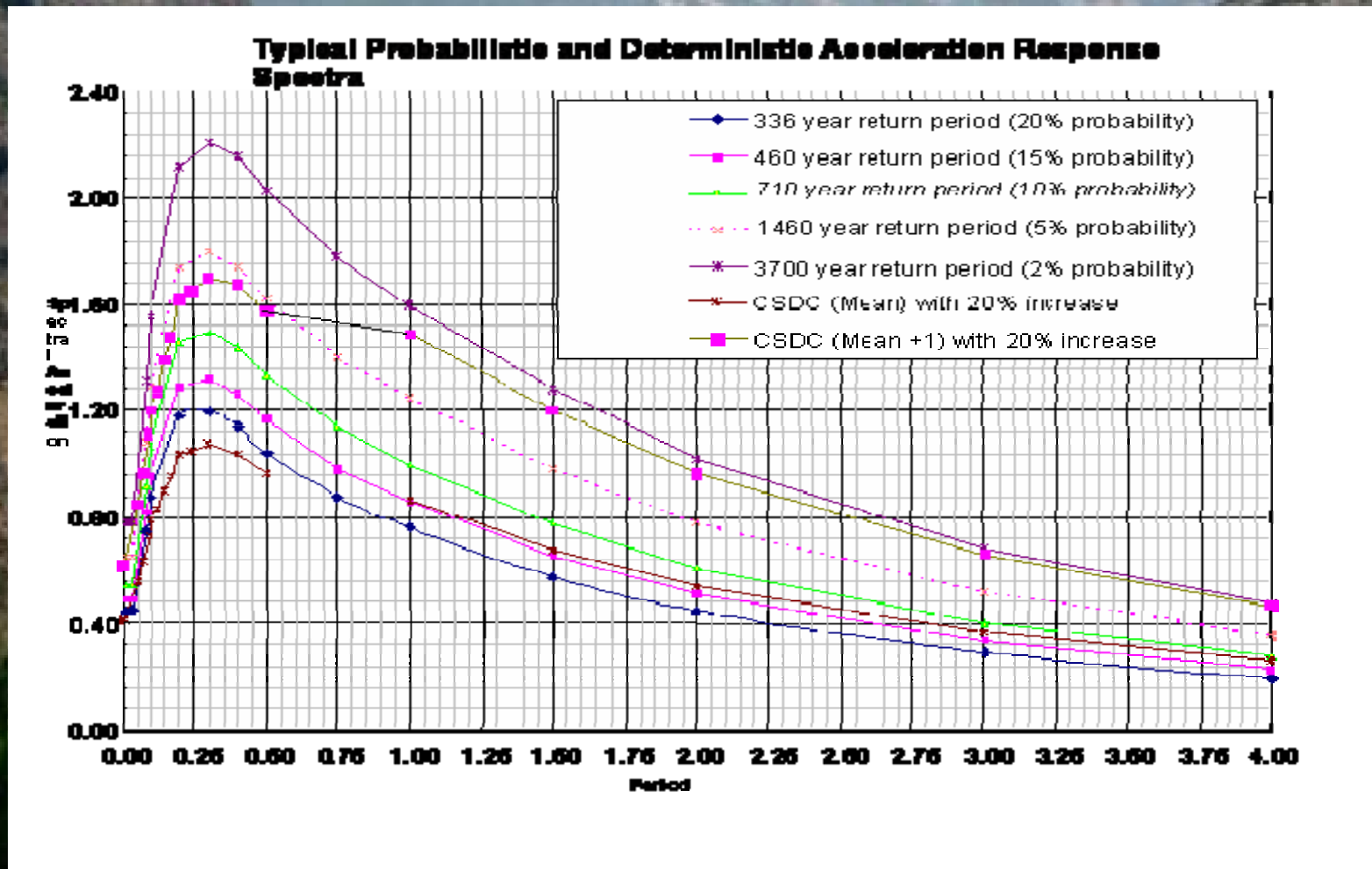
EXAMPLE # 2

6 Foot Column Diameter/CIDH Test Specimen (UCLA)



EXAMPLE # 2

Probabilistic Acceleration Response Spectra San-Francisco the Bay Area Region Marina



EXAMPLE # 2

Analytical Study of 6 Foot Circular Column/CIDH

Assuming $10\% f'c Ag$ Axial Load

DAMAGE INDEX

| ARS risk of Occurrence (%) | Return Period (Yrs) | Δ_p | Δ_y | T | a (ARS) | Δ_D | Δ_{uc} | Damage |
|----------------------------|---------------------|------------|------------|------|---------|------------|---------------|--------|
| | | (in) | (in) | sec | (g) | (in) | (in) | DI |
| (Mean) | N/A | 57.73 | 9.86 | 2.22 | 0.52 | 25.2 | 68.00 | 0.26 |
| (Mean +1) | N/A | 57.73 | 9.86 | 2.22 | 0.92 | 44.60 | 68.00 | 0.60 |
| 20 | 336 | 57.73 | 9.86 | 2.22 | 0.40 | 19.38 | 68.00 | 0.16 |
| 15 | 460 | 57.73 | 9.86 | 2.22 | 0.47 | 22.77 | 68.00 | 0.22 |
| 10 | 710 | 57.73 | 9.86 | 2.22 | 0.54 | 26.16 | 68.00 | 0.28 |
| 5 | 1460 | 57.73 | 9.86 | 2.22 | 0.72 | 34.88 | 68.00 | 0.43 |
| 2 | 3700 | 57.73 | 9.86 | 2.22 | 0.96 | 46.51 | 68.00 | 0.63 |

A scenic view of a mountain valley with a bridge in the distance. The foreground shows rocky, sparsely vegetated slopes. In the middle ground, a multi-arched bridge spans across a valley. The background features more mountain ranges under a cloudy sky.

Next Steps...

- Calibration of *DI* using data from tests and post-event observations
- Development of a reliability index covering damage and probabilistic demand
- Local vs. Global *DI* (redundancy)
- Extension of *DI* application to repair projects in order to facilitate communication between maintenance and design

A photograph of a large stone arch bridge spanning a deep canyon. The bridge features a prominent central arch and several smaller arches on either side. The surrounding landscape is rugged and rocky, with some greenery visible in the lower left. The sky is overcast with light clouds. The word "Questions" is written in orange text across the upper middle of the image, and a large white question mark is centered over the bridge's main arch.

Questions

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